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The extraordinary case of the lightest strange resonance J. R. Peláez

Non perturbatoive QCD 2016. Sevilla. 21st October 2016

From naive quark model: quark-antiquark states

With only 3 light quarks, grouped in SU(3) nonets



qq⁻Mass hierarchy:

These heavier because m_s>>m_u~m_d Not for plarst

Follow linear (J,M²) Regge trajectories



Linear (J,M²) trajectories with Universal slope ~ 0.8-1 GeV⁻² (Also for baryons)

Rigid rotating rod, Stringy picture Color flux tube... CONFINEMENT

Note no scalars there

But the very existence of some light scalars is under debate Mild fading

controversy

Let us first see HOW MANY SCALARS EXIST (in the PDG) below 2 GeV:

• Isospin=0: $\sigma/f_0(500)$ $f_0(980)$, $f_0(1370)$ $f_0(1500)$, $f_0(1700)$ 5 states.

Half century-long controversy **Settled.** (Even at PDG)

Isospin=1: a₀(980), a₀(1450).

3x2=6 states

• I=1/2, S=±1 $\kappa/K_0^*(800)$ $K_0^*(1430)$

4x2=8 states

40 yr-long controversy Almost Settled but omitted from PDG summary tables. According to PDG: "Needs Confirmation"

19 states... enough to form TWO NONETS And something more.

The lightest ones should form the lightest nonet.

- Scalar SU(3) multiplets identification controversial
 - Too many resonances for many years. But there is an emerging picture...





Enough f_0 states have been observed: $f_0(500)$, $f_0(980)$, $f_0(1370)$, $f_0(1500)$, $f_0(1700)$. The whole picture is complicated by mixture between them (lots of works here) The light scalar controversy. The theory side... NON-ORDINARY nature

By ORDINARY we mean "quark-antiquark", but there are other possibilities

- Tetraquarks (Jaffe '77) .Solves the inverted hierarchy problem (issues with chiral symmerty and excess of states),
 PROBLEM WITH SEMILOCAL DUALITY
- Molecules (Achasov, Jülich-Bonn, Oller-Oset) are also NON-ORDINARY,... May also have problem with semi-local duality
- Modified quark-antiquark models with meson interactions, Van Beveren, Rupp
- Some people claim/claimed some of these did/do not exist, like the very σ, the κ(800), the f₀(1370),etc...
 (Minkowski, Ochs, Narison... σ as glueball supporters in general)



For decades, only data from

Kπ scattering. But no Breit-Wigner peak

Extremely wide resonance



Usually quoted by its pole:

$$\sqrt{s_{pole}} \approx M - i \Gamma / 2$$

Poles are process independent, peaks are **NOt**

Starting in the 2000's until today

Decays from heavier mesons Fermilab E791, Focus, Belle, KLOE, BES,...

Very good statistics Clear initial states and different systematic uncertainties.

Strong experimental claims for wide and light σ around 500 MeV

"Strong" experimental claims for wide and light κ around 800 MeV

Very convincing for PDG, but personal caveats on BW parametrizations used, which may affect the precision and meaning of the pole parameters

The $\sigma/f_0(500)$: similar situation, but made it to the PDG in 1996 and well established in 2002 and major revisión for precisión in 2012

Part of the problem: The theory

Many old an new studies based on crude/simple models,

Strong model dependences Suspicion: What you put in is what you get out??

Even experimental analysis using

WRONG theoretical tools contribute to confusion

(Breit-Wigners, isobars, K matrix,)

Let's revisit how the EXISTENCE of the σ was settled and if the same can be done with the κ

Fortunately, **DISPERSIVE FORMALISMS** provide the correct analytic structure, precise AND MODEL INDEPENDENT analyses CAUSALITY: Partial waves t(s) are ANALYTIC in complex s plane with cuts due to thresholds (also in crossed channels

Cauchy Theorem determines t(s) at ANY s, from an INTEGRAL on the contour

If t->0 fast enough at high s, curved part vanishes

$$t(s) = \frac{1}{\pi} \int_{th}^{\infty} \frac{Im t(s')}{s - s'} ds' + LC$$



Otherwise, determined up to polynomial (subtra

Good for: 1) Calculating t(s) where there is not data

2) Constraining data analysis

3) ONLY MODEL INDEPENDENT extrapolation to complex s-plane

Unitarized ChPT

90's Truong, Dobado, Herrero, JRP, Oset, Oller, Ruiz Arriola, Nieves, Meissner,...

Use ChPT amplitudes inside dispersion relation. Relatively simple, although different levels of rigour. Generates all scalars. Crossing (left cut) approximated..., not good for precision but good for understanding parameters

Solutions of Roy-like equations.

70's Roy, Basdevant, Pennington, Petersen...

00's Ananthanarayan, Caprini, Colangelo, Gasser, Leutwyler, Moussallam, Decotes Genon, Lesniak, Kaminski...

Left cut implemented with precision . Use data on all waves + high energy + ChPT for subtraction constants

 $\sigma_{pole} \approx (441^{+16}_{-8}) - i(272^{+9}_{-12.5}) MeV$

Caprini, Colangelo, Leutwyler (2006)

Data Analyses constrained with Roy & Forward Disperion Relations.

García-Martín, Kaminski, JRP, Ruiz de Elvira, Yndurain 00's

Left cut implemented with precision Use data on all waves at all energies. NO ChPT.

 $\sigma_{pole} \approx (457^{+14}_{-15}) - i(279^{+11}_{-7}) MeV$

These two methods good for precision. Game changers for PDG

The consistency of dispersive approaches, and also with previous results implementing UNITARITY, ANALTICITY and chiral symmetry constraints by many people ...

(Ananthanarayan, Caprini, Bugg, Anisovich, Zhou, Ishida Surotsev, Hannah, JRP, Kaminski, Loiseau, Lesniak,Oller, Oset, Dobado, Tornqvist, Schechter, Fariborz, Saninno, Van Beveren, Rupp, Zou, Zheng, etc....)

... led the PDG to neglect those works not fullfilling these constraints also restricting the sample to those consistent with NA48/2, together with results from heavy meson decays Finally quoting in the 2012 PDG edition...

> M=400-550 MeV Γ=400-700 MeV

Accordingly THE NAME of the resonance was changed to...



DRAMMATIC AND LONG AWAITED CHANGE ON "sigma" RESONANCE @ PDG!!



Actually, in PDG 2012: "Note on scalars" One might also take the more radical point of view and just average the most advanced dispersive analyses, Refs. [8–11], shown as solid dots in Fig. 1, for they provide a determination of the pole positions with minimal bias. This procedure leads to the much more restricted range of $f_0(500)$ parameters

$$\sqrt{s_{\text{Pole}}^{\sigma}} = (446 \pm 6) - i(276 \pm 5) \text{ MeV}$$
.



For a FANTASTIC review by a very recomendable author

From controversy to precision on the sigma meson: a review on the status of the non-ordinary f0(500) resonance. J.R.P. arXiv:1510.00653. Phys.Rept. in press

8. G. Colangelo, J. Gasser, and H. Leutwyler, NPB603, 125 (2001).
9. I. Caprini, G. Colangelo, and H. Leutwyler, PRL 96, 132001 (2006).
10. R. Garcia-Martin, R. Kaminski, JRP, J. Ruiz de Elvira, PRL107, 072001(2011).

11. B. Moussallam, Eur. Phys. J. C71, 1814 (2011).

But why not the kappa??

"omitted from the summary table" since, "needs confirmation"

But, all descriptions of data respecting unitarity and chiral symmetry find a pole at M=650-770 MeV and Γ ~550 MeV or larger.

As for the σ, the best determination comes from a SOLUTION of a Roy-Steiner dispersive formalism, consistent with UChPT Decotes Genon et al 2006

PDG dominated by such a SOLUTION

M-i Γ/2=(682±29)-i(273±i12) MeV @PDG2015

 $K_0^*(800)$ Situation similar to the sigma before the 2012 revision

PDG willing to consider it confirmed.. if additional independent dispersive DATA analysis.

We have been encouraged

by PDG members to do it.





We (A.Rodas & JRP) are working on a

Dispersive analysis of πK scattering DATA

(not a solution of dispersión relations, but a constrained fit)

First observation: Forward Dispersion relations Not well satisfied by data Particularly at high energies

So we use Forward Dispersion Relations as CONSTRAINTS on fits S-waves. The most interesting for the kappa



From Unconstrained (UFD) to Constrained Fits to data (CFD)



From Unconstrained (UFD) to Constrained Fits to data (CFD)

D-waves: Largest changes of all, but at very high energies



Regge parameterizations allowed to vary: Only πK - ρ residue changes by 1.4 deviations



We have amplitudes that describe data and satisfy dispersion relations up to 1.6 GeV

THERE IS A KAPPA POLE Extracted from conformal parameterization Preliminary and STILL MODEL DEPENDENT

M-i Γ/2=(680±15)-i(334±i15) MeV

Compare to PDG: M-i Γ/2=(682±29)-i(273±i12) MeV

Still in progress:

We are planning to extract it in a model Independent way with rigorous analytic methods and also imposing Roy-Steiner dispersion relations, as done for the sigma. IN PROGRESS

We expect this second dispersive determination will finally settle the $\kappa/K_0^*(800)$ issue at the PDG.

Now, about the kappa non-ordinary nature

1) Non linear Regge trajectory

2) Large Nc from UChPT Already discussed 4 years ago at this meeting

Regge Theory and Chew-Frautschi Plots

All hadrons are classified in almost linear (J,M²) trajectories

Intuitively like a quark-antiquark pair confined at the ends of a string-like/flux-tube configuration.

ALL OF THEM? Not quite...

are doubled due to two flavor components, nn and ss. We do not put the enigmatic σ meson [11–14] on the $q\overline{q}$ trajectory supposing σ is alien to this classification. The broad state

M², GeV²

SeV²

π,(2390)/6

π(1300)

π(1800)

m2(2070

m2(1670)

Pm.(2360)

(a)

03(2510)

os(2070)

(b)

a (2,450)

a,(2100)

a,(1640)

a,(1/230)

3

And the K₀*(800) is NOT EVEN MENTIONED

Linear trajectories due to of some specific dynamics OTHER DYNAMICS MAY LEAD TO OTHER TRJECTORIES



Anisovich-Anisovich-Sarantsev-Phys.Rev.D62.051502-4

Introduction: Regge Theory

The Regge trajectories can be understood from the analytic extension to the complex angular momentum plane of the partial wave expansion through the Sommerfeld-Watson transform:

$$T(s,t) = \sum_{J=0}^{\infty} (2J+1) f_J(s) P_J(z) \longrightarrow T(s,t) = -\frac{1}{2i} \int_C \frac{(2J+1) f(J,s) P_J(-z)}{\sin \pi J} dJ$$



Introduction: Regge Theory



The contribution of a single Regge pole to a partial wave, is shown to be

$$f(J,s) = \hat{f} + \frac{\beta(s)}{J - \alpha(s)}$$

"background" regular function. Assumption: WE WILL AVOID IT in our cases by going to the pole

Parametrization of amplitudes dominated by Regge pole

Chu, Epstein, Kaus, Slansky, Zachariasen, PR175, 2098 (1968).

Moreover, for meson-meson scattering:

Unitarity condition on the real axis implies

$$\operatorname{Im}\,\alpha(s) = \rho(s)\beta(s)$$

$$\rho(s) = \sqrt{1 - 4m_\pi^2/s}$$

• Further properties of $\beta(s)$

threshold behavior

$$\beta(s) = \frac{\hat{s}^{\alpha(s)}}{\Gamma(\alpha(s) + \frac{3}{2})} \gamma(s)$$

$$\hat{s} = \frac{s - 4m^2}{\tilde{s}}$$

suppress poles of full amplitude

$$(2\alpha+1)P_{\alpha}(z_s) \sim \Gamma(\alpha+\frac{3}{2})$$

analytic function: $\beta(s)$ real on real axis \Rightarrow phase of Y(s) known \Rightarrow Omnès-type disp. relation

Parametrization of Regge pole dominated amplitudes

(Already presented in the 2014 edition of this meeting)

The trajectory and residue should satisfy these integral equations:

$$\operatorname{Re}\alpha(s) = \alpha_0 + \alpha's + \frac{s}{\pi}PV\int_{4m_\pi^2}^{\infty} ds' \frac{\operatorname{Im}\alpha(s')}{s'(s'-s)},$$

$$\begin{aligned} \operatorname{Im}\alpha(s) &= \rho(s)b_0 \frac{\hat{s}^{\alpha_0 + \alpha' s}}{|\Gamma(\alpha(s) + \frac{3}{2})|} \exp\left(-\alpha' s [1 - \log(\alpha' \tilde{s})]\right) \\ &+ \frac{s}{\pi} PV \int_{4m_\pi^2}^{\infty} ds' \frac{\operatorname{Im}\alpha(s') \log \frac{\hat{s}}{\hat{s}'} + \arg\Gamma\left(\alpha(s') + \frac{3}{2}\right)}{s'(s' - s)} \end{aligned}$$

Different interactions have different constants In the scalar case a slight modification is introduced (Adler zero)

Constants fixed by forcing the amplitude to have THE POLE AND RESIDUE OF THE DESIRED RESONANCE



INPUT for our purposes: **The ρ pole**:

$$\rho_{pole} \approx 763_{-1.5}^{+1.7} - i73.2_{-1.1}^{+1.0} \text{MeV} \qquad |g| = 6.01_{-0.07}^{+0.04}$$

Results: *p* case (*I* = 1, *J* = 1)



We (black) recover a fair representation of the partial wave, in agreement with the GKPY amplitude (red)

Neglecting the "background" vs. Regge pole gives a 10-15% error.

Particularly in the resonance region

Fair enough to look for the Regge trajectory

Results: *p* case (I = 1, J = 1)

We get a prediction for the ρ Regge trajectory, which is almost real



Almost LINEAR $\alpha(s) \sim \alpha_0 + \alpha' s$

intercept α_0 = 0.520±0.002

slope $\alpha' = 0.902 \pm 0.004 \text{ GeV}^{-2}$

Previous studies from FITS: [1] $\alpha_0 = 0.5$ [1] $\alpha' = 0.83 \text{ GeV}^{-2}$ [2] $\alpha_0 = 0.52 \pm 0.02$ [2] $\alpha' = 0.9 \text{ GeV}^{-2}$ [3] $\alpha_0 = 0.450 \pm 0.005$ [4] $\alpha' = 0.87 \pm 0.06 \text{ GeV}^{-2}$

Remarkably consistent with the literature!!, (taking into account our approximations)

[1] A. V. Anisovich et al., Phys. Rev. D 62, 051502 (2000)
[2] J. R. Pelaez and F. J. Yndurain, Phys. Rev. D 69, 114001 (2004)
[3] J. Beringer et al. (PDG), Phys. Rev. D86, 010001 (2012)
[4] P. Masjuan et al., Phys. Rev. D 85, 094006 (2012)

$f_2(1275)$ and $f_2'(1525)$ cases (I = 0, J = 2)

J.A. Carrasco J.Nebreda, JRP, A. Szczepaniak, Phys.Lett. B749 (2015) 399

Almost elastic: $f_2(1275)$ BR ($\pi \pi$) = 85% and $f_2'(1525)$ BR(KK)=90%. Solving the integral equations we "predict" again:



The "prediction" for the rho trajectory was known since the 70's, we have just updated it and obtained new "predictions" for the f_2 and f_2 '

So, once we have checked that our approach predicts the established Regge trajectories just from the pole position and residue...

What about the $\sigma/f_0(500)$ and $K^*_0(800)$?

INPUT: Analytic continuation to the complex plane of a dispersive analysis of data



INPUT for our purposes: **The** σ **pole**:

$$(457_{-15}^{+14}) - i(279_{-7}^{+11})$$
MeV

$$|g| = 3.59^{+0.11}_{-0.13} \,\mathrm{GeV}$$

Results: *σ case (I = 0, J = 0)*



Somewhat better agreement in the resonance region of the Regge pole dominated amplitude with the dispersive amplitude.

So, we apply a similar procedure but now for the $f_0(500)$

Results: *o case* (*I* = 0, *J* = 0)

The prediction for the σ Regge trajectory, is:



• NOT approximately real

NOT linear

interceptslope $\alpha_{\sigma}(0) = -0.090^{+0.004}_{-0.012},$ $\alpha'_{\sigma} \simeq 0.002^{+0.050}_{-0.001} \, {\rm GeV^{-2}}$

Compare with the rho result...

$$\alpha_0 = 0.52$$
 $\alpha' = 0.913 \text{ GeV}^{-2}$

The sigma does **NOT** fit the ordinary meson trajectory

Two orders of magnitude flatter than other hadrons Typical of meson physics? F_{π} , m_{π} ?



Ordinary $\rho(770)$ trajectory $\alpha_0 = 0.52$ $\alpha' = 0.913 \text{ GeV}^{-2}$ The $\sigma/f_0(500)$ trajectory is **not real** and much smaller $\alpha_{\sigma}(0) = -0.090^{+0.004}_{-0.012},$ $\alpha'_{\sigma} \simeq 0.002^{+0.050}_{-0.001} \text{ GeV}^{-2},$

The σ trajectory is **NOT** ordinary No evident Regge partners

Much flatter than other hadrons. Another scale at play. Meson physics involved? F_{π} , m_{π} ?

Results: *σ case (I = 0, J = 0)*

IF WE INSISTED in fixing the α ' to an "ordinary" value ~ 1 GeV⁻² and the trajectory to a straight line...



The data description would be severely spoilt

And now the trajectories with strangeness

The K*(892) case (I = 1/2, J = 1)

Very elastic to $K\pi$. Different masses now. Slight modification Solving the integral equations we "predict" again:



The $K_{1}^{*}(1400)$ case (I = 1/2, J = 1)

Very elastic to $K^*\pi$, BR=94±6%. Decays to a resonance+pion Solving the integral equations we "predict" again:



The $K_0^*(1430)$ case (I = 1/2, J = 0)

Quite elastic to $K\pi$, BR=93±10%. Many models predict quark-antiquark with sizable mixing to $K\pi$. Solving the integral equations we "predict" again:



The kappa case (I = 1/2, J = 0)

JRP, A.Rodas in preparation

Elastic to $K\pi$. Cryptoexotic candidate Solving the integral equations we "predict":



Results: *k* case (I = 1/2, J = 0)

IF WE INSISTED in fixing the α ' to an "ordinary" value ~ 1 GeV⁻² and the trajectory to a straight line...



The data description would be severely spoilt If not-ordinary...

What then? Can we identify the dynamics of the σ and κ trajectories?

Not quite yet... but...

Ploting the trajectories in the complex J plane...



Striking similarity with Yukawa potentials at low energy: V(r)=-Ga exp(-r/a)/r

Our result is mimicked with a=0.5 GeV⁻¹ to compare with S-wave $\pi\pi$ scattering length 1.6 GeV⁻¹

"a" rather small !!!

The extrapolation of our trajectory also follows a Yukawa but deviates at very high

Results: *k* case (I = 1/2, J = 0)

For the kappa we find a very similar behavior to the sigma:



Compared to: V(r)=-Ga exp(-r/a)/r

Similar order of magnitude for range

a_{ππ}=0.5 GeV⁻¹ a_{πK}=0.33 GeV⁻¹

a_{ππ}/ a_{πK} ~1.52

Maybe a_{MM} scales as inverse of reduced mass

$$\mu_{\pi K} \, / \, \mu_{\pi \pi} = 1.57$$

Summary

Part 1

The use of good data and MODEL INDEPENDENT DISPERSIVE methods were essential to establish the $\sigma/f_0(500)$ parameters

The $\kappa/K_0^*(800)$ is now in a similar situation as the $\sigma/f_0(500)$ in 2010. We are working to have an additional DISPERSIVE DETERMINATION that will confirm its parameters.

For the moment we have $K\pi$ amplitudes consistent with Forward Dispersion Relations and data up to 1.6GeV. Naive extrapolation gives consistent kappa pole. Rigorous pole extraction coming. Expect changes @PDG soon.

Part 2

Using dispersive approach we can CALCULATE the Regge trajectories of elastic resonances. The ρ , K^{*}, f2, f2' and K₁ result in the usual linear trajectories.

But the $\sigma/f_0(500)$ and $\kappa/K_0^*(800)$ do not fit into conventional linear Regge trajectories. They behave similarly and have scales typical of meson physics