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# Correction of optic disc measurements on fundus photographs* 

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#### Abstract

If defined as diameter of image/diameter of object, the magnification $M$ of the eye-camera system is $k B$, where $k$ is a camera constant and $B$ represents the vergence of the internal axis of the eye. The magnification may be assessed (1) from the length $l$ of the eye, using the formula $1.336 k /(l-0.0016)$; (2) from the glass refraction $G$, using the formula $k \bar{D} /(1-G / \bar{D})$, in which $\bar{D}$ is the " normal" refractive power of the eye; or (3) from the principal point refraction $A$ and the deviation $\Delta D_{1}$ from the "normal" refractive power of the cornea, using the formula $k \bar{D} \cdot(1+\Delta B / \bar{D})$, where $\Delta B=A+0.84$ $\Delta D_{1}$. If $k$ is 0.042 m , as in the Zeiss camera, and $\bar{D}$ is about 60 dpt , the formulas may be written as (1) $M=$ $0.056 /(l-0.0016) ;$ (2) $M=2.5 /(1-0.017 G)$; and (3) $M=2.5 \cdot(1+0.017 \Delta B)$.


## Introduction

Blurred disc margins are common in small dises, and many large discs are pale or show high cup: disc ratios. Therefore, the question as to whether a certain optic nerve head is oedematous, atrophic, glaucomatous or normal often leads to the question as to whether the optic disc is small, large or medium-sized. The latter question, however, is nearly always left without an answer. A major reason for this seems to be that correction of optic disc measurements is considered to be necessary but intricate and cumbersome.

It is impossible to place a measuring rod directly on the fundus of the living eye. Information concerning the size of an optic nerve head must be obtained by measurements on an image of the optic disc rather than on the disc itself. The image is usually much larger than its object, and variations in the size of the image may be

[^0]caused by variations in the degree of magnification as well as in the size of the object. Indeed, apparent interindividual variations in optic dise size were long supposed to be predominantly spurious rather than true. Uncorrected length measurements on disc photos are deeply mistrusted despite their being strongly correlated to their corrected counterparts [1, 3, 5].

A simple factor, $(1-0.017 G)$, in which $G$ represents the glass refraction, was used by Bengtsson [3] to correct optic disc measurements on fundus photos. A comprehensive derivation of this factor was provided 1977 by Bengtsson and Krakau [4] in a paper on some essential features of the Zeiss fundus camera, in which the authors stressed a remarkable fact, namely, that the magnification is entirely dependent on the vergence of the internal axis. The refraction and the corneal curvature are involved only as means of estimating this quantity when actual measurements of the axial length are not available.

In 1982 Littman [6] published a method for correction based on measurements of the principal point refraction and corneal curvature: by means of a system of curves, one obtains a correction factor $q$, which can in turn be corrected using similar curves based on measurements of the length of the optical axis of the eye. In a second paper, Littman [7] fitted quadratic equations to the curves.

In the present paper we describe simple equations by which the magnification of the eye-camera system can be estimated (1) directly from measurements of the internal axis of the eye, (2) from the glass refraction or (3) from the principal point refraction and the corneal curvature. The first two estimations seem to be suitable for practical purposes; the third enables us to compare the results of our approach with those obtained by Littman.

## The magnification

In all discussions of the design and function of optical instruments, Gullstrand's exact schematic eye is always the starting point. Careful measurements on normal eyes


Fig. 1. Gullstrand's exact schematic eye


Fig. 2. Formation of an image of a retinal object: $M_{\text {eye }}=h_{e} / h_{\mathrm{r}}=(1 /$ $A+1 / D) /(1 / D)=(D+A) / A=B / A$
of the curvature and position of surfaces separating structures with different refractive indices are summarized in a model to which the well-known formulas of Gaussian (ordinary geometric) optics can be applied. From Fig. 1 it can be seen that there are six cardinal points: two are focal ( $F_{1}$ and $F_{2}$ ), two are principal ( $P_{1}$ and $P_{2}$ ), and two are nodal ( $N_{1}$ and $N_{2}$ ). Distances are counted to or from the nearest principal point and are reduced, i.e. divided by the refractive index of the pertinent medium. Formulas and calculations are further simplified if distances (expressed in metres) are substituted by vergences, i.e. by their inverted values (expressed in diopters). An example is provided by Gullstrand's formula $B=D+A$, in which $A$ stands for the principal point refraction - i.e. the power of a hypothetical correction glass located in the anterior principal plane of the eye $-D$ represents the refractive power of the eye, and $B$ stands for the vergence of the internal axis - i.e. the reduced and inverted distance between the posterior principal point and the fovea. (If written $A=B-D$, this
formula shows that the principal point refraction is equal to the difference between the vergence of the internal axis and the refractive power.)

Using this notation, the magnification of the eye is $M_{\text {eye }}=B / A$ (Fig. 2), that of the fundus camera is $M_{\text {camera }}=k A$ (Fig. 3) and that of the eye-camera system, therefore, is
$M=k B$
If the camera is correctly positioned in relation to the patient, $k$ is a constant and the magnification is a linear function of $B$. A comprehensive derivation of Eq. (1) was provided in a previous paper [4].

Equation (1) may be written $k=M / B$ and be used to calculate $k$ from measurements of the magnification on fundus photos of an artificial eye in which $B$ is known. If, as in the Zeiss camera, 1 dm on a measuringtape situated 0.5 m behind a $+2-\mathrm{dpt}$ lens yields an image measuring 8.4 mm , the "magnification" is $0.084, B$ is 2 dpt and $k$, accordingly, is $0.084 / 2=0.042 \mathrm{~m}$.

## Estimate based on ultrasonography

In the human eye, $B$ may be calculated from measurements of the axial length $l$ with the aid of the formula $B=n /(l-p)$, in which $n$ is the refractive index and $p$ is the distance from the apex of the cornea to the posterior principal point. Using Eq. (1), we obtain $M=n k /(l-$ $p$ ) or, if we disregard small variations in $p$ and insert $n=1.336$ and $p=0.0016$,
$M_{e 1}=1.336 \mathrm{k} /(\mathrm{l}-0.0016)$
If, for instance, $k=0.042$ and $l=0.024$, we obtain $M=$ 2.5 and may conclude that an image with a diameter of 4 mm is derived from an object with a diameter of $4 / 2.5=1.6 \mathrm{~mm}$.

## Estimate based on glass refraction

If measurements of the internal axis are not available, $B$ may be estimated using Gullstrand's formula $B=D+$ $A$, inserting an observed value for $A$ and accepting a "normal" value $\bar{D}$ for $D$. Thus, the estimated magnifica-


Fig. 3. The imaging system of the Zeiss fundus camera: $M_{\text {camera }}=h_{c} / h_{e}=$ $\left[f_{f} /(1 / A+d)\right] \cdot\left[f_{c} d(1+d A)\right] / f_{f}^{2}=\left(f_{c} d / f_{f}\right) A=$ $k A$. Reproduced with permission from Acta Opthalmologica
tion is $M_{e 2}=k(\bar{D}+A)$, which may be written as $M_{e 2}=$ $k \bar{D}(1+A / \bar{D})$ or, since $(1+A / \bar{D})=1 /(1-G / \bar{D})$ if the distance from the test glass to the anterior principal plane of the eye is $1 / \bar{D}$, as recommended by Gullstrand,
$M_{e 2}=k \bar{D} /(1-G / \bar{D})$.
If $k=0.042$ and $\bar{D}$ is about 60 dpt , we obtain
$M_{e 2}=2.5 /(1-0.017 G)$.

## Estimate based on refraction and keratometry

The total refractive power $D$ of the eye is composed of the refractive powers $D_{1}$ and $D_{2}$ of the cornea and lens, respectively. Only the corneal power is easily measured. $D_{1}$ and $D_{2}$ are not simply additive (since $D=D_{1}+$ $D_{2}-\delta D_{1} D_{2}$, where $\delta$ is the effective depth of the anterior chamber) and are probably not uncorrelated. The change in $D$ associated with a deviation $\Delta D_{1}$ from the "normal" refractive power $\bar{D}_{1}$ of the cornea, therefore, is $\beta \Delta D_{1}$ where $\beta$ is the coefficient of regression of $D$ on $D_{1}$. Thus, the estimate of $B$ is $\left(\bar{D}+A+\beta \Delta D_{1}\right)$ and that of the magnification is
$M_{e 3}=k\left(\bar{D}+A+\beta \Delta D_{1}\right)$.
Since $\beta=r \cdot \sigma y / \sigma x$, the figures given by Stenström [12] can be used to calculate an approximate value $\beta=r_{D_{1} D}$. $\sigma D / \sigma D_{1}=0.66 \cdot 1.78 / 1.40=0.84$. The insertion of $\beta=$ $0.84, k=0.042$ and $\bar{D}=58.64$ (as in Gullstrand's exact schematic eye) in Eq. (5) yields
$M_{e 3}=0.042\left(58.64+A+0.84 \Delta D_{1}\right)$,
which, if $\left(A+0.84 \Delta D_{1}\right)$ is replaced by $\Delta B$, may be written as
$M_{e 3}=2.46(1+0.017 \Delta B)$.

## Comparison with Littman's approach

## Deduction of q

Littman $[6,7]$ describes the diameter $t$ of a retinal object as being a product of the observed diameter $s$ of the image, the camera constant 1.37, and a factor $q$ :
$t=s \cdot 1.37 \cdot q$.
Since $t / s=1 / M, q=0.73 / M$.
The introduction of Eq. 7 for $M$ yields
$q=0.73 /[2.46(1+0.017 \Delta B)]=0.297 \cdot 1 /(1+x)$,
where $x=0.017 \Delta B$. However,
$1 /(1+x)=1-x+x^{2}-x^{3}+x^{4} \ldots$
This series is convergent if the absolute value of $x$ is $<1$. In the relevant range, $0.017 \Delta B$ is so small that three terms are sufficient to give a good approximation of $q$. Hence,
$100 q=29.7-0.5 \Delta B+0.009(\Delta B)^{2}+R$,

|  | $r(\mathrm{~mm})$ | $B \Delta D_{1}$ (dpt) | Range of $A(\mathrm{dpt})$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\square$ | 6.0 | 10.4 | -30.0 to +5.0 |  |
| + | 7.7 | 0.0 | -25.0 | to +10.0 |
| 0 | 10.0 | -8.4 | -20.0 | to +15.0 |



Fig. 4. Comparison of the numerical values of $0.73 / q\left(=M_{\text {Littman }}\right)$ and $0.042\left(58.64+A+0.84 \Delta D_{1}\right)\left(=M_{e 3}\right)$ for different combinations of refraction and corneal curvature

Sources of variation:
Remedies:
Measureme
definition,
projection,
centering and
eye-to-camera distance


True optic disc diameter (80\%)

Fig. 5. Schematic representation of relative sizes of different components of the interindividual variance in optic disc-diameter measurements
which is similar to the quadratic equations provided by Littman [7].

## Transformation of Littman's curves

Conversely, the equation $q=0.73 / M$ may be written as $M=0.73 / q$ and be used, together with the formula for the refractive power of the cornea ( $D_{1}=0.336 / r$ ), to transform Littman's curves into almost straight lines

Table 1. Symbol, value, derivation and denomination of constants and variables

| A | $G /(1-G / \bar{D}) \mathrm{dpt}$ | Principal point refraction of the eye |
| :---: | :---: | :---: |
| $B$ | $n /(l-p) \mathrm{dpt}$ | Vergence of the internal axis of the eye |
| $\Delta B$ | $\left(A+\beta \Delta D_{1}\right) \mathrm{dpt}$ | Estimated deviation of $B$ from $\bar{D}$ |
| $\beta$ | 0.84 (Stenström) | Coefficient of regression of $D$ on $D_{1}$ |
| D | $(B-A) \mathrm{dpt}$ | Total refractive power of the eye |
| $\bar{D}$ | 58.64 dpt (Gullstrand) | "Normal" refractive power of the eye |
| $D_{1}$ | 0.336/r dpt | Refractive power of the cornea |
| $\bar{D}_{1}$ | $0.336 / \bar{r} \mathrm{dpt}$ | "Normal" refractive power of the cornea |
| $\Delta D_{1}$ | $\left(D_{1}-\bar{D}_{1}\right) \mathrm{dpt}$ | Deviation of $D_{1}$ from $\bar{D}_{1}$ |
| $D_{2}$ | $\left(D-D_{1}\right) /\left(1-\delta D_{1}\right) \mathrm{dpt}$ | Refractive power of the crystalline lens |
| $\delta$ | 0.0043 m (Gullstrand) | Effective depth of the anterior chamber ${ }^{\text {a }}$ |
| G | measured (dpt) | Glass refraction |
| $k$ | measured (m) | Camera constant ${ }^{\text {c }}$ |
| l | measured (m) | Distance from the apex of the cornea to the retina |
| M | $k B$ | Magnification of the eye-camera system |
| $M_{e 1}$ | $n k /(1-p)$ | First estimate of $M$ |
| $M_{e 2}$ | $k \bar{D} /(1-G / \bar{D})$ | Second estimate of $M$ |
| $M_{e 3}$ | $k \bar{D} \cdot(1+\Delta B / \bar{D})$ | Third estimate of $M$ |
| $n$ | 1.336 (Gullstrand) | Refractive index of the eye |
| $p$ | 0.0016 m (Gullstrand) | Distance from the apex of the cornea to the posterior principal point |
| $q$ | $\begin{aligned} & 0.01\left(a A^{2}-b A+c\right) \\ & \mathrm{mm} /{ }^{\circ} \end{aligned}$ | Correction factor of Littman ${ }^{\text {b }}$ |
| $r$ | measured (m) | Corneal radius |
| $\bar{r}$ | 0.0077 m (Gullstrand) | "Normal" corneal radius |
| $s$ | measured (mm) | Diameter of the image of the eye-camera system |
| $t$ | $\begin{aligned} & (s / M) \mathrm{mm} \text { or } \\ & (s \cdot u \cdot q) \mathrm{mm} \end{aligned}$ | Diameter of the retinal object |
| $u$ | $(0.0573 / \mathrm{k})^{\circ} / \mathrm{mm}$ | Camera constant of Littman ${ }^{\text {c }}$ |

${ }^{\text {a }}$ Reduced distance between the principal planes of the cornea and the crystalline lens
${ }^{\mathrm{b}} a, b$ and $c$ vary with $r$
${ }^{\text {c }}$ In the Zeiss camera $k=0.042$ and, thus, $u=1.37$
that may be approximated by the following expression:
$M=2.45(1+0.018 \Delta B)$,
which is similar to (7).

## Graphic comparison

The values of $0.73 / q\left(=M_{\text {Littman }}\right)$ and $0.042(58.64+A+$ $\left.0.84 \Delta D_{1}\right)\left(=M_{e 3}\right)$ for different combinations of refrac-
tion and corneal curvature are compared in Fig. 4, which shows an excellent agreement between the two.

## Discussion

Littman's graphs are the result of trigonometric calculations that are not further specified and, therefore, not easy to check. They have been suspected by Quigley et al. [11] of underestimating the disc diameter. However, it is reassuring that Littman's results agree with ours. It is indeed possible that Gullstrand's value for $\bar{D}(58.64 \mathrm{dpt})$ is too low and that 60 dpt is a more realistic figure. This would make estimates of the disc diameter that are not based on actual measurements of the internal axis even lower.

Choices between different methods of correction should be based on accurate information about different sources of error. Figure 5 gives a schematic overview based on information provided by Stenström [12], Bengtsson [3], Balazsi et al. [1], Jonas et al. [5] and Mansour [9].

According to Stenström [12], variations in lens power are slightly more important $\left(r_{D D_{2}}=0.7\right)$ than variations in corneal power ( $r_{D D_{1}}=0.66$ ), even in persons aged $<35$ years. Age-related lens changes should be expected to increase this difference. Mansour's results [9] seem to indicate that variations in lens power are almost twice as important as variations in corneal power. Measurements of the corneal curvature are therefore hardly rewarding for the present purpose.

If correction for the influence of the glass refraction is considered to be unsatisfactory, correction based on measurements of the axial length seems to be the only alternative. However, if ultrasonography is to make sense, other errors must be rectified as well. The camera has to be correctly positioned in relation to the patient [8], and the optic disc must be centered in the photographic field [2, 10]. Photography, projection, tracing and planimetry should be repeated and the results, averaged [5]. Nevertheless, small but inevitable errors arising from many sources are added up; moreover, as there is no way to check the outcome, excessive expectations of exactness will remain unrewarded. Therefore, the use of a method that is comprehensible and easy to practise is the only reasonable approach.

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