



# COVID 19



Nuevas dinámicas del mercado laboral tras el confinamiento en Andalucía: el empleo del futuro post-Covid 19 y respuesta a nuevos confinamientos

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# Evaluating the long-term impacts of economic or policy shocks among necessity and opportunity entrepreneurs

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## Abstract

We aim at distinguishing between two categories of self-employed workers based on revealed intentions (necessity versus opportunity entrepreneurs), equating hysteresis with the existence of a unit root in a variable whether aggregate rates of entrepreneurship exhibit persistence or hysteresis, and finally use longer time horizons in formal evaluation exercises rather than the few years which are commonly used to gauge entrepreneurship policy impacts. Our analysis includes a timewise analysis of persistence, checks for nonlinear patterns and finally models regime switching behavior for the afore-mentioned groups.

- JEL: C32 E23 J24 M13
- Keywords: necessity entrepreneurs; transition regression model; hysteresis and stochastic components: nonlinearities; unit roots

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## 1 Introduction

The dynamics of the self-employment rate during the business cycle keep being a source of controversy among scholars, summarized in the so-called push and pull hypotheses [1], as well as in the distinction between opportunity and necessity entrepreneurs [2], as two different components of business creation with potentially opposite dynamics over the business cycle. Empirical estimates of the self-employment/unemployment relationship only aspired to capture a “net” effect of the recession-push and the prosperity-pull effects [3]. However, recent literature has provided operational definitions of opportunity and necessity entrepreneurship using readily available nationally representative data [4]-[5], applying time series techniques for checking the macro-dynamics of opportunity and necessity self-employment during the business cycle [6]-[7]. With different targets –contributions to innovation and economic growth or as an alternative of other ALMP’s– governments, around the world, have devised and implemented portfolios of policies to promote entrepreneurship (more appropriate opportunity entrepreneurs) or to turn unemployment into self-employment (more appropriate for necessity motivated entrepreneurs). These interventions impose sizeable costs on the taxpayer. For this reason, these policies (in both the short and long term) should be properly monitored and evaluated. Recent studies have evaluated national experiences employing register data by using different outcomes such as duration into self or regular employment, incomes or job satisfaction [8]. In general, this literature appears to point at the positive results of start-up programs for unemployed and underline higher probabilities of survival among opportunity entrepreneurs. [9]. However, and due to data limitations, the long-run effects are not accurately captured by conventional evaluations, which are usually performed a few years after the policies are implemented, and so capture only short-term impacts. There exists, however, an alternative path: exploring the macro-dynamics of self-employment, in particular whether entrepreneurship evolves as a trend stationary or as a non-stationary time-series process. If entrepreneurship is trend stationary, economic and policy shocks can

be regarded as transitory from an aggregate perspective: the rate of entrepreneurship eventually reverts to its underlying, long-run rate. If, on the other hand, the rate of entrepreneurship is non-stationary, such shocks will have permanent effects. With this in mind, and to the best of our knowledge this paper represents the first attempt to evaluate the long run effects of positive shocks in the self-employment due to push factors, at the macro-level. Sapin is a suitable case of study since e.g. the use of entrepreneurship promotion as an active labor market policy has been intensively applied as a way to combat unemployment. By using a new data set of regional time series of necessity entrepreneurs for the 17 Spanish regions, our results point to the existence of hysteresis. As the main analysis entails unit root testing in a time series environment, we decided to employ panel unit root testing with alternative heterogeneous hypotheses, robust to both classical spherical disturbances and eventual spatial spillovers, in order to check for the robustness of the main results. Finally, our analysis adds to the national and regional level estimates an additional layer of complexity by estimating nonlinear models of convergence in five different economic sectors, agriculture, industry, low and high skilled services.

## 2 Data

Data are drawn from the quarterly microdata 2000/1 to 2020/4 of the Spanish Labor Force Survey (EPA). The Survey, conducted by the National Statistical Institute (INE), is a large household sample survey providing results on labor participation of people aged 16 and over as well as persons outside the labor force in which each sampled individual remaining in the survey for a period of six quarters at a time, with no resampling after individuals are rotated out of the sample.

The Survey is targeted at a rotating sample of around 60,000 households throughout the national territory. For every household member, both socio-economic and labor information is collected in order to summarize the main characteristics of the Spanish workforce each quarter. Individuals in the sample are interviewed for six consecutive quarters, thus we have information on quarterly labor transitions for a maximum period of 18 months for each individual in the sample.

Following Fairlie and Fossen [4]-[5] we will define necessity entrepreneurs as self-employed who answered their previous labor force status question as “out of the labor force but able to work”. In contrast, opportunity entrepreneurs were those individuals whose status was ‘in the labor force’ and they had been “employed” for either a public or private institution preceding their current self-employment status.

By using this approach once the two categories of self-employed workers are identified, and applying the elevation factors, we built the national aggregate quarterly time series of necessity and opportunity entrepreneurs and a panel data for the 17 Spanish regions.

After applying the necessary filters to the data, our panel contains a total

of 11,849,287 individual observations. For each of the above mentioned groups, each time series has been disaggregated by Spanish regions and, for each region, by: 1) the duration of the unemployment period prior to the transition to self-employment (only for necessity entrepreneurs); 2) the educational attainment level; and 3) the economic sector observed in self-employment transition.

We define a necessity entrepreneur in quarter  $t$  as an individual who experiences a transition towards self-employment state between quarters  $t$  and  $t + 1$ , conditional on being observed in quarter  $t$  in a non-employment state (either by being classified as unemployed -actively seeking employment-, or as inactive). In contrast, we define an opportunity entrepreneur in quarter  $t$  as an individual who experiences a transition towards self-employment state between quarter  $t$  and  $t + 1$ , conditional on being observed in quarter  $t$  in an employment status other than self-employment (i.e. wage employees, both in the public and private sector).

Therefore, the total number of individuals transiting to self-employment state between quarter  $t$  and  $t+1$  is composed of those come from non-employment state (necessity entrepreneurs) and those who come from employment state (opportunity entrepreneurs). Based on this, we analyze the share of each of these two types of entrepreneurs over the total at each quarter.

### 3 Methodology

Our analysis entails a unit root and stationarity testing of the raw variables. Through a series of Dickey Fuller based tests and considering both a linear and a nonlinear alternative [10]-[11], we test for the presence of persistent behavior (stochastic trends) in a series of quarterly observations spanning the 2000 - 2020 period. As a second step, we make use of the Hansen test [12], in its panel rendition, to check for possible alternatives to non linearity by comparing a sequence of F tests based on the null hypothesis of non linearity against the possible alternative of possible existing branches, namely up to two. We then test for possible discrete regime switching behavior –Threshold autoregression models (TAR) and self exciting threshold autoregression models (SETAR) [13] – by selecting an array of possible weakly exogenous threshold variables (unemployment in level, changes in unemployment, GDP growth rate) and endogenous ones (time lagged self-employment variables such as the number of necessity or opportunity entrepreneurs). Robustness of the unit root analysis is checked through Panel unit root tests which allow for heterogeneous hypothesis testing (relaxing the hypothesis of a single coefficient across all cross sections [14]-[15]), while possible asymmetries are checked via the aforementioned Hansen Panel test as in Terasvirta et al. [16].

## 4 Unit root Analysis

### 4.1 Hysteresis analysis: national and regional level

To have some decisive understanding of our strategy, in our paper we shall:

- Employ the Perron-Vogelsang and Clemente et al. unit root tests against the one and two breaks alternative hypothesis
- Verify and test for ex-ante Panel time series linearity against nonlinear, multiple-branched alternatives
- Select models for our threshold analysis with Information Criteria minimization against their linear specification
- Employ an ADF type test equation with an attractor to fit the TAR and SETAR modelling in order to test for different speed of return to unconditional mean
- Make a simple, initial educated guess: let the transition regression speed be dominated by the level of unemployment (**and later by a GDP growth indicator**)

$$\Delta nec_t = c + \rho nec_{t-1} + e_t \quad (1)$$

As the hysteresis hypothesis represents a crucial component of our work, we have chosen to check for the robustness of the one and two breaks unit root models by employing an additional unit root test with multiple convenient properties. To be more specific, we choose to select a second generation panel unit root test, capable of taking into account possible cross sectional correlation, to countercheck the results of time series testing. Our choice ultimately fell on the Im, Pesaran and Shin unit root test and Hadri's stationarity test. The latter was chosen as it presents an inverted null of stationarity, takes possible correlation in the error terms of the cross sections into account and even more importantly present an heterogeneous alternative instead of a standard homogeneous one (meaning that the null hypothesis implies all cross sections are stationary while the alternative states that some cross sections contain unit roots). We reckon such choices and strategies would end up being adequate to our set up (17 different autonomous regions with different economic structures), considering homogeneity across regions members of the country on top of time variation.

### 4.2 Some insight on Unit Root testing

In our paper, we employ both additive and innovation model specifications from Perron and Vogelsang unit root break test. The main difference between the two specifications is that the innovation model entails a less sudden change in

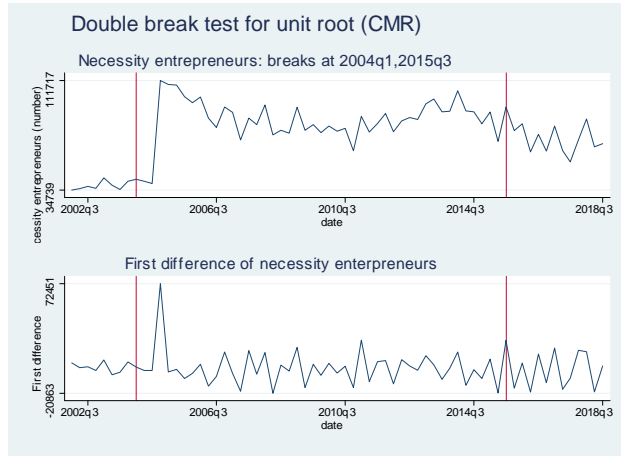


Figure 1: Unit Root test, two breaks, necessity entrepreneurs

the level relationship, while the additive model, which we would focus on given the results of visual inspection, would present an alternative based on a sharper change of the intercept.. The test equation below (2) would thus represent a unit root testing with a nested alternative of a break in the constant.

$$nec_t = \mu + \theta DU_t(T_b) + \alpha nec_{t-1} + \sum_{j=1}^k c_j \Delta nec_{t-j} + w_t \quad (2)$$

The Perron-Vogelsang is perhaps a common test in literature. In order to accommodate a systematic shift in our data and to avoid data mining<sup>1</sup>, we choose to extend the analysis with an additional test, which would add a second deterministic break in levels. Such test is basically a generalization from Clemente-Montañes-Reyes of the already cited Perron-Vogelsang test, and its test equation is visible in (eq-3).

$$nec_t = \mu + \theta_1 DU_{1,t}(T_{a,t}) + \theta_2 DU_{2,t}(T_{b,t+s}) + \alpha nec_{t-1} + \sum_{j=1}^k c_j \Delta nec_{t-j} + w_t \quad (3)$$

In both Equations 2 and 3, the homogeneous hypothesis will thus be  $H_0 : \alpha = 0$  against a heterogeneous null  $H_a = \alpha < 0$ .

### 4.3 Perron-Vogelsang results with a single break

For the remainder of the paper, we shall use the following numbering to indicate the autonomous communities of Spain and the country as a whole: 1, Andalusia;

<sup>1</sup>On such issue, please have a look at Figure 1 to Figure 4. The data we could retrieve from EPA allowed us to build series with a systematic level change in 2004. In order to check for consistency of results across same unit root testing applications and considering the somewhat limited length of our time series we necessarily had to resort to up to two break alternatives.

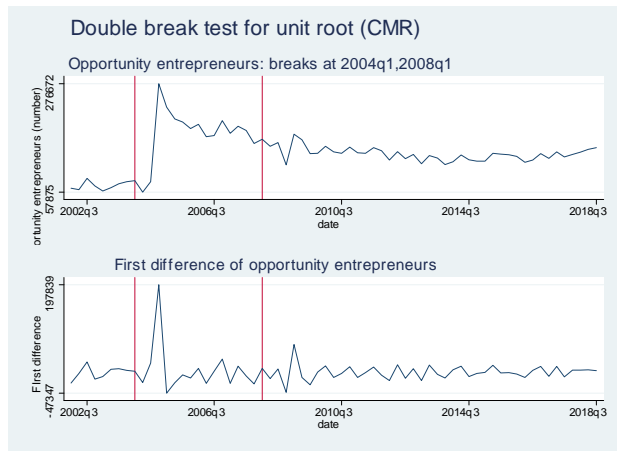


Figure 2: Unit Root test, two breaks, opportunity entrepreneurs

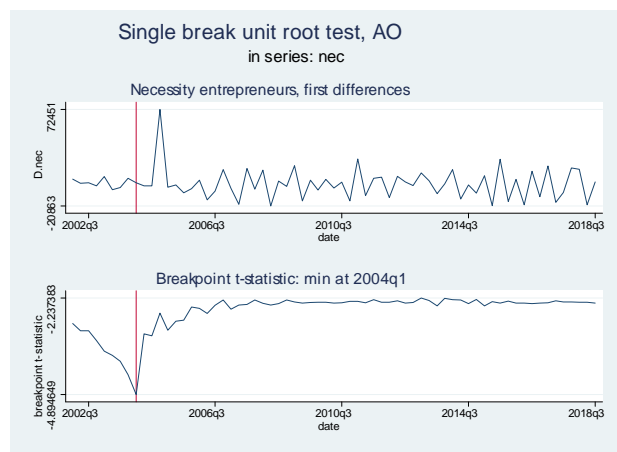


Figure 3: Unit root test, one break, AO, necessity workers



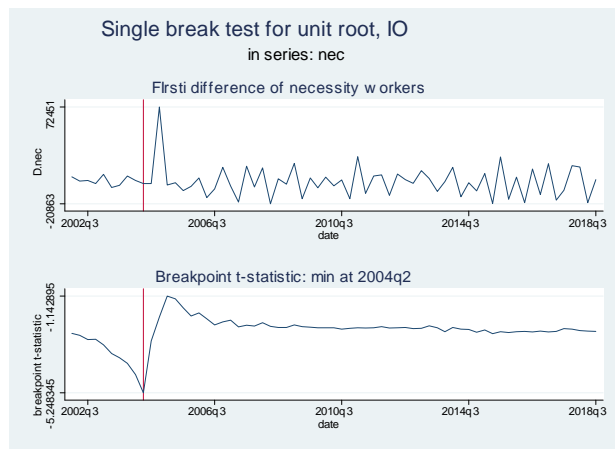


Figure 4: Unit root test, one break, IO, necessity workers

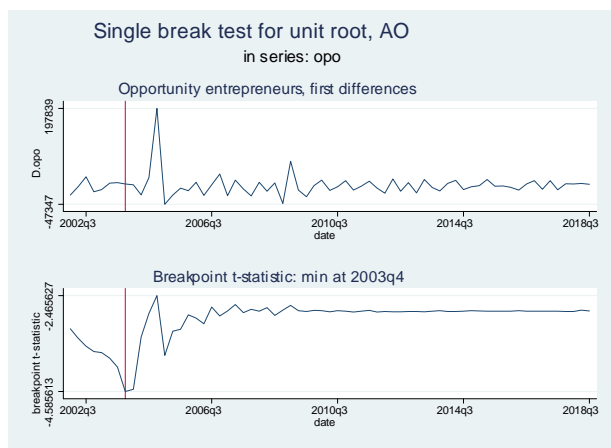


Figure 5: Unit root test, one break, AO, opportunity entrepreneurs

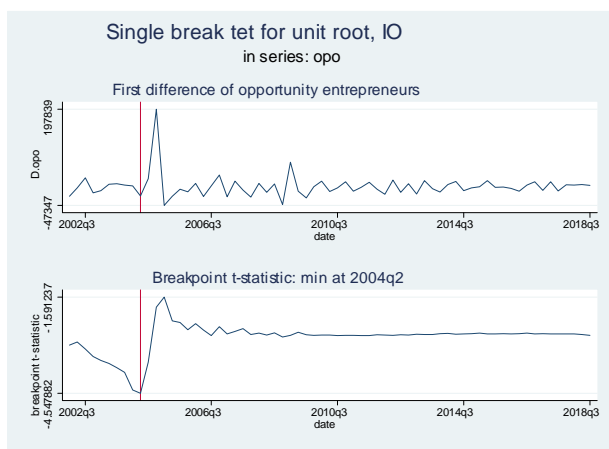


Figure 6: Unit root test, one break, IO, opportunity workers

2, Aragon; 3, Asturias; 4, Balearic Islands; 5, Canary Islands; 6, Cantabria; 7, Castile and Leon; 8, Castile and La Mancha; 9, Catalonia; 10, Valencian Community; 11, Extremadura; 12, Galicia; 13, Community of Madrid; 14, Murcia; 15, Navarre; 16, Basque Country; 17, La Rioja; 18, Spain as a whole.

Let's consider the innovation outlier first: for the necessity entrepreneurs variable, the hypothesis of unit root with one break could not be rejected at 5% in Cantabria, Castile-la Mancha, Valencia, Galicia and Madrid (6 8 10 12 13) while it was generally accepted elsewhere in the country. As for the opportunity entrepreneurs variable, the null of nonstationarity was found to be generally unrejected in Andalucia, Asturias, Cantabria, Murcia, Navarre and the Basque Country (1 3 6 14 15 16). Most expectedly, unemployment was never found to be stationary and breakdates for the alternatives would be closely contained between the 2007q3 and the 2008q3 interval.

The additive outlier, on the other side, gave us the following results: in the case of necessity entrepreneurs, Andalucia, Asturias, Cantabria, Castile and Leon, Castile-La Mancha, Extremadura, Galicia, Madrid, the Basque Country and the whole country series could not see the null of unit root rejected for an alternative with a sudden change structure (1 3 6 7 8 11 12 13 16 18). As for opportunity entrepreneurs, the majority of the regions, Andalucia, Aragon, Asturias, Balearic isl., Castile and Leon, Castile-La Mancha, Catalonia, Valencia, Extremadura, Madrid, Murcia, Navarre, Basque Country and the whole country series were considered  $I(1)$  by the test (1 2 3 4 7 8 9 10 11 13 14 15 16 18). As with the IO model, unemployment appears to be absolutely nonstationary at 5% in any given region.

Table 1: Unit Root tests, AO, one break, Necessity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
(I)	(II)	(III)	(IV)	(V)
<i>Andalusia</i>	-4,968*	4,129		-4,270
<i>Aragon</i>	-8,093*	3,715		-4,270
<i>Asturias</i>	-7,629*	3,609		-4,270
<i>Balearic Islands</i>	-4,859*	3,881		-4,270
<i>Canary Islands</i>	-5,374*	4,134		-4,270
<i>Cantabria</i>	-3,729	1,520		-4,270
<i>Castile and Leon</i>	-8,224*	4,163		-4,270
<i>Castile-La Mancha</i>	-3,325	2,512		-4,270
<i>Catalonia</i>	-8,237*	5,894		-4,270
<i>Valencian Community</i>	-3,844	3,107		-4,270
<i>Extremadura</i>	-8,472*	3,485		-4,270
<i>Galicia</i>	-1,824	-2,602		-4,270
<i>Community of Madrid</i>	-4,132	3,411		-4,270
<i>Region of Murcia</i>	-10,370*	4,862		-4,270
<i>Navarre</i>	-7,330*	-1,475		-4,270
<i>Basque Country</i>	-4,506*	3,467		-4,270
<i>La Rioja</i>	-9,126*	3,784		-4,270
<i>SPAIN</i>	-5,579*	4,599		-4,270

Unit root tests. P values of the endogenously retrieved breaks reported. One break case.

Table 2: Unit Root tests, AO, one break, Necessity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
(I)	(II)	(III)	(IV)	(V)
<i>Andalusia</i>	-3,388	8,850		-3,560
<i>Aragon</i>	-8,040*	3,814		-3,560
<i>Asturias</i>	-1,793	4,544		-3,560
<i>Balearic Islands</i>	-4,448*	4,856		-3,560
<i>Canary Islands</i>	-6,338*	5,477		-3,560
<i>Cantabria</i>	-3,248	2,919		-3,560
<i>Castile and Leon</i>	-0,376	4,242		-3,560
<i>Castile-La Mancha</i>	-2,471	5,258		-3,560
<i>Catalonia</i>	-4,531*	8,703		-3,560
<i>Valencian Community</i>	-7,948*	6,289		-3,560
<i>Extremadura</i>	-3,440	3,850		-3,560
<i>Galicia</i>	-1,252	2,990		-3,560
<i>Community of Madrid</i>	-1,170	7,893		-3,560
<i>Region of Murcia</i>	-7,159*	4,005		-3,560
<i>Navarre</i>	-8,042*	2,841		-3,560
<i>Basque Country</i>	-2,944	5,045		-3,560
<i>La Rioja</i>	-9,230*	3,984		-3,560
<i>SPAIN</i>	-2,269	11,273		-3,560

Unit root tests. P values of the endogenously retrieved breaks reported. One break case.

Table 3: Unit Root tests, IO, one break, Opportunity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
(I)	(II)	(III)	(IV)	(V)
<i>Andalusia</i>	-3,280	-1,763		-4,270
<i>Aragon</i>	-6,199*	3,640		-4,270
<i>Asturias</i>	-4,101	2,721		-4,270
<i>Balearic Islands</i>	-8,527*	4,447		-4,270
<i>Canary Islands</i>	-4,476*	2,333		-4,270
<i>Cantabria</i>	-3,315	1,343		-4,270
<i>Castile and Leon</i>	-5,327*	2,926		-4,270
<i>Castile-La Mancha</i>	-5,554*	3,535		-4,270
<i>Catalonia</i>	-8,099	6,177		-4,270
<i>Valencian Community</i>	-6,515*	4,511		-4,270
<i>Extremadura</i>	-5,620*	2,429		-4,270
<i>Galicia</i>	-4,536*	2,817		-4,270
<i>Community of Madrid</i>	-7,056*	6,658		-4,270
<i>Region of Murcia</i>	-3,476	-3,319		-4,270
<i>Navarre</i>	-3,779	2,495		-4,270
<i>Basque Country</i>	-3,487	2,562		-4,270
<i>La Rioja</i>	-8,473*	5,603		-4,270
<i>SPAIN</i>	-5,311*	4,020		-4,270

Unit root tests. P values of the endogenously retrieved breaks reported. One break case.

Table 4: Unit Root tests, AO, one break, Opportunity entrepreneurs

Regions	t-stat	Break 1 p-value	Break 2 p-value	5% crit
<i>Andalusia</i>	-3.190	4.872		-3.560
<i>Aragon</i>	-1.051	5.962		-3.560
<i>Asturias</i>	-2.374	3.601		-3.560
<i>Balearic Islands</i>	-2.641	5.288		-3.560
<i>Canary Islands</i>	-4.874*	4.364		-3.560
<i>Cantabria</i>	-6.415*	1.751		-3.560
<i>Castile and Leon</i>	-1.801	5.421		-3.560
<i>Castile-La Mancha</i>	-2.199	6.447		-3.560
<i>Catalonia</i>	-3.399	9.367		-3.560
<i>Valencian Community</i>	-2.586	7.448		-3.560
<i>Extremadura</i>	-2.503	4.136		-3.560
<i>Galicia</i>	-4.603*	2.550		-3.560
<i>Community of Madrid</i>	-1.950	7.677		-3.560
<i>Region of Murcia</i>	-1.998	-2.732		-3.560
<i>Navarre</i>	-3.297	3.800		-3.560
<i>Basque Country</i>	-3.014	5.880		-3.560
<i>La Rioja</i>	-5.769*	7.660		-3.560
<i>SPAIN</i>	-2.241	8.158		-3.560

Unit root tests. P values of the endogenously retrieved breaks reported. One break case.

#### 4.4 Clemente-Montañes-Reyes with two breaks

Let us turn our attention to the 2 breaks model: In the case of the necessity entrepreneurs, the null hypothesis is not rejected for Asturias, Balearic islands, Cantabria, Castile-La Mancha, Valencia, Galicia and the Basque Countries (3 4 6 8 10 12 16) with the innovation outlier model at 5%. As for the more sudden change implied by the additive outlier model, again in the case of necessity entrepreneurs, the null hypothesis is not rejected for Aragon, Balearic Islands, Canary Islands, Castile and Leon, Castile-La Mancha, Catalonia, Extremadura, Galicia, Madrid, Murcia, Basque Country and La rioja (2 4 5 7 8 9 11 12 13 14 16 18) with the additive outlier model at 5%. Given the sudden sharp change we could detect by the means of a preliminary visual inspection, we reckon the last model would be indeed more representative of the true process underlying the series for the necessity entrepreneurs group. In the case of the opportunity entrepreneurs, the innovative outlier test fails to reject the unit root against two deterministic jumps in the mean in Navarre only, while the additive outlier test states that regions Aragon, Asturi, Cantabria, Castile and Leon, Castile-La Mancha, Catalonia, Valencia, Galicia, Murcia, Navarre and the Basque Country (2 3 6 7 8 9 10 12 14 15 16 18) could not reject the unit root against the deterministic hypothesis at the 5% percent significance level. In general, the endogenously retrieved break dates point at the first quarter of 2004 and at the neighborhood of 2008 as the suggested jump dates. As the first date presents a generally sharper shift in the relationship and is more closely connected to the nature of the data, the second one would most likely connect to the financial crisis period, thus disconnecting the causes of the long memory process from the exogenous impact of the sub-prime and subsequent economic crisis in the European Area. Unsurprisingly, the unemployment rate was found to be nonstationary in almost every region, with the retrieved break dates pointing at 2008 and 2015 respectively.

Table 5: Unit Root tests, IO, two breaks, Necessity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
(I)	(II)	(III)	(IV)	(V)
Andalusia	-9,486*	7,433*	-4,742	-5,490
Aragon	-8,300*	-3,657	-0,743	-5,490
Asturias	-4,451	3,687	-1,244	-5,490
Balearic Islands	-5,094	3,985	1,467	-5,490
Canary Islands	-9,375*	5,639	-3,935	-5,490
Cantabria	-3,407	2,735	-1,979	-5,490
Castile and Leon	-10,188*	6,052	-4,090	-5,490
Castile-La Mancha	-3,850	3,204	-1,879	-5,490
Catalonia	-7,211*	6,254	-3,647	-5,490
Valencian Community	-4,901	4,295	-3,032	-5,490
Extremadura	-9,474*	8,051	-6,824	-5,490
Galicia	-4,368	5,291	-6,187	-5,490
Community of Madrid	-9,969*	7,476	-4,366	-5,490
Region of Murcia	-11,136*	6,135	-3,121	-5,490
Navarre	-8,007*	3,008	-3,352	-5,490
Basque Country	-4,502	4,918	-3,224	-5,490
La Rioja	-9,311*	3,224	0,688	-5,490
SPAIN	-8,991*	8,053	-5,888	-5,490

Unit root tests. P values of the endogenously retrieved breaks reported. Two breaks case.

Table 6: Unit Root tests, AO, two breaks, Necessity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
(I)	(II)	(III)	(IV)	(V)
Andalusia	-8,442*	8,095	-2,704	-5,490
Aragon	-2,774	2,961	0,921	-5,490
Asturias	-6,954*	4,787	-1,786	-5,490
Balearic Islands	-3,403	4,023	1,331	-5,490
Canary Islands	-4,596	6,957	-4,106	-5,490
Cantabria	-10,326*	3,337	-1,708	-5,490
Castile and Leon	-4,668	5,050	-2,996	-5,490
Castile-La Mancha	-3,120	5,023	-0,528	-5,490
Catalonia	-5,184	9,439	-2,730	-5,490
Valencian Community	-8,817*	7,005	-2,683	-5,490
Extremadura	-3,565	5,497	-3,645	-5,490
Galicia	-1,635	6,425	-5,315	-5,490
Community of Madrid	-5,132	9,288	-3,899	-5,490
Region of Murcia	-2,503	5,673	-2,795	-5,490
Navarre	-6,589*	3,279	-1,765	-5,490
Basque Country	-1,492	5,594	-2,795	-5,490
La Rioja	-9,246*	3,042	1,001	-5,490
SPAIN	-4,380	13,533	-4,773	-5,490

Unit root tests. P values of the endogenously retrieved breaks reported. Two breaks case.

Table 7: Unit Root tests, IO, two breaks, Opportunity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
(I)	(II)	(III)	(IV)	(V)
Andalusia	-8,282*	8,203	-8,457	-5,490
Aragon	-7,579*	6,861	-6,284	-5,490
Asturias	-10,409*	7,748	-6,118	-5,490
Balearic Islands	-9,407*	5,558	-3,049	-5,490
Canary Islands	-8,228*	4,992	-3,811	-5,490
Cantabria	-10,020*	7,145	-6,495	-5,490
Castile and Leon	-10,059*	8,859	-7,968	-5,490
Castile-La Mancha	-6,784*	-6,892	-7,180	-5,490
Catalonia	-10,550*	8,768	-5,190	-5,490
Valencian Community	-7,751*	9,250	-7,285	-5,490
Extremadura	-10,194*	7,665	-7,206	-5,490
Galicia	-7,435*	8,160	-7,127	-5,490
Community of Madrid	-8,572*	8,949	-5,746	-5,490
Region of Murcia	-9,447*	5,454	-5,894	-5,490
Navarre	-5,180	6,364	-5,937	-5,490
Basque Country	-7,662*	7,600	-7,091	-5,490
La Rioja	-10,090*	7,366	-4,398	-5,490
SPAIN	-12,664*	11,930	-10,383	-5,490

Unit root tests. P values of the endogenously retrieved breaks reported. Two breaks case.

Table 8: Unit Root tests, AO, two breaks, Opportunity entrepreneurs

<i>Regions</i>	<i>t-stat</i>	<i>Break 1 p-value</i>	<i>Break 2 p-value</i>	<i>5% crit</i>
<i>Andalusia</i>	-8,225*	9,855	-7,719	-5,490
<i>Aragon</i>	-2,222	8,558	-5,179	-5,490
<i>Asturias</i>	-2,492	8,336	-4,882	-5,490
<i>Balearic Islands</i>	-7,681*	5,964	-2,432	-5,490
<i>Canary Islands</i>	-8,130*	5,217	-2,883	-5,490
<i>Cantabria</i>	-3,488	5,596	-4,449	-5,490
<i>Castile and Leon</i>	-3,195	9,504	-6,353	-5,490
<i>Castile-La Mancha</i>	-4,894	9,139	-5,298	-5,490
<i>Catalonia</i>	-4,110	10,037	-3,135	-5,490
<i>Valencian Community</i>	-5,393	9,143	-4,437	-5,490
<i>Extremadura</i>	-7,692*	7,723	-6,094	-5,490
<i>Galicia</i>	-3,482	7,939	-5,563	-5,490
<i>Community of Madrid</i>	-8,434*	8,113	-2,671	-5,490
<i>Region of Murcia</i>	-3,145	5,569	-5,810	-5,490
<i>Navarre</i>	-1,909	5,066	-3,145	-5,490
<i>Basque Country</i>	-3,486	8,103	-4,714	-5,490
<i>La Rioja</i>	-6,919*	7,528	-3,372	-5,490
<i>SPAIN</i>	-2,948	12,076	-6,261	-5,490

Unit root tests. P values of the endogenously retrieved breaks reported. Two breaks case.

Table 9: Unit Root tests, National level

	<i>t</i>	<i>Break 2 p-value</i>	<i>Break 2 p-value</i>	<i>5 % critical value</i>	
	(I)	(II)	(III)	(IV)	(V)
<i>nec<sub>t</sub></i>					
<i>AO 1 break</i>	-2,27	0,00			-3,56
<i>IO 1 break</i>	-5,58*	0,00			-4,27
<i>AO 2 breaks</i>	-4,38	0,00	0,00		-5,49
<i>IO 2 breaks</i>	-9,00*	0,00	0,00		-5,49
<i>opo<sub>t</sub></i>					
<i>AO 1 break</i>	-2,24	0,00			-3,56
<i>IO 1 break</i>	-5,31*	0,00			-4,27
<i>AO 2 breaks</i>	-2,94	0,00	0,00		-5,49
<i>IO 2 breaks</i>	-12,66*	0,00	0,00		-5,49

Unit root tests. P values of the endogenously retrieved breaks reported. One and two breaks hypothesis.

## 4.5 Results of the hysteresis analysis at the national level

National level results are merged and showed jointly in Table 9. As we have stated previously, the innovative outlier model easily rejects the unit root hypothesis with flying colors. However, considering how sudden changes in employment would appear by visual inspection and considering the width of the series, the additive outlier specification appears to be unable to do so in both one and two break model tests. In order to make up our mind and to be able to take a final decision on the overall hysteresis phenomenon in the country as a whole, we would have to resort to a counter-test to act as a robustness check. That is exactly what we shall see in the section dedicated to the panel unit root tests.

## 4.6 Sectorial analysis at the autonomous regional level

We finally test for unit root behavior at the sectorial level, to provide some understanding on how the hysteresis phenomenon behaves across Agriculture, Industry, Construction, Low Qualified Services and High Qualified Services.

Given the initial results of the unit root analysis for the regions as a whole, we now look at the sectorial evolution of the memory process for the necessity entrepreneurs group focusing in particular on the additive outlier model. That

appears considering the outcome of our previous inspections (visual and stability analysis) to be the choice most suited to the nature of our data.

Starting with the necessity entrepreneurs group and in the first sector, agriculture, we could not reject the unit root null for the level variables in 2 7 8 9 11 12 15 18. As for the second sector, the industrial one, unit root behavior was found in 4 15 16 17. As we switch our attention to the construction sector, testing for a unit root shows that regions 5 8 10 18 would have indeed a unit root hidden in their DGP. Let us complete the analysis of the necessity entrepreneurs group with the service sector, as we can distinguish between low skilled and high skilled entrepreneurs in this instance. For the share of the service sector requiring less qualified labor, a unit root was found in 1 2 3 5 10 12 13 14 18. Finally, high skilled labor led to non rejection of the unit root hypothesis in 12 and 15 only.

Let us focus on the opportunity entrepreneurs group now. In the agricultural sector, regions 3 7 9 11 15 17 18 showed evidence of unit root behavior. As for the industrial sector, we confirmed a unit root in 2 3 5 8 11 12 13 16 18. In the construction sector, 2 3 4 8 12 18 were found to show a unit root behavior. Finally, in the low and high skill service sectors, regions 1 2 3 4 7 11 13 15 16 18 presented a unit root for the former sector and 5 and 16 only for the latter. What indeed appears striking is the strong degree of persistence found in low skilled labor sectors, which is in relative terms much less present in the high skilled sector.

As a single break alternative naturally suits our data by construction, it is crucial for us to add and compare the results illustrated in the last paragraph with a two deterministic breaks alternative. We thus employ once more the Clemente et al. extending the previous analysis once more to all available in regions across all sectors with a sharp change as implied by the additive outlier model.

As before, let us focus once again on the necessity entrepreneurs first. For the agricultural sector, 1 4 6 7 8 9 10 11 12 15 18 showed a unit root process with probability values frequently lower than one percent. For the industry sector, the series for 1 3 4 5 6 10 11 12 14 15 17 were seen as integrated by the test. In the case of the construction sector, series 2 5 7 8 9 10 11 15 17 18 contained a unit root. Finally, for the low skilled service sector and the high skilled service sector, series 3 4 5 10 15 17 18 appear to be integrated of order one for the former, while series 3 6 8 11 14 15 appear to be integrated of order one for the latter.

Let's finally turn our attention to the opportunity entrepreneurs series: in the agricultural sector, 2 4 6 7 8 9 10 11 12 13 15 16 17 18 presented a unit root. In the industrial sector, a non stationary process could be confirmed for 2 3 7 9 13 14 16 17 18. Switching to construction, we find a unit root process in the opportunity entrepreneurs series for 1 2 4 8 9 10 12 14 17 18. Turning our view to the service sector, in the case of the low qualified services, we have decisive evidence of a unit root process in 2 3 4 6 7 9 10 11 12 15 16 18. Finally, for the higher skilled labour force in the service sector, we have evidence of a unit root process in 4 5 6 7 11 12 13 16 17 18.

Table 10: Unit Root tests, homogeneous alternative, CSC and heteroskedasticity, Panel

(I)	Test (II)	$H_0$ (III)		$H_a$ (IV)	Heteroskedasticity (V)	CSS (VI)	Statistic (VII)	p-value (VIII)
$\Delta opot$	Hadri	Hom. Stationarity	Het. Unit Root		Robust	Robust	-4.10	1.00
$opot$	Hadri	Hom. Stationarity	Het. Unit Root		Robust	Robust	16.10*	0.00
$\Delta nec_t$	Hadri	Hom. Stationarity	Het. Unit Root		Robust	Robust	-4.22	0.00
$nec_t$	Hadri	Hom. Stationarity	Het. Unit Root		Robust	Robust	22.26*	0.00
$\Delta opot$	IPS	Hom. Unit Root	Het. Stationarity		Robust	Demeaned	-31.44*	0.00
$opot$	IPS	Hom. Unit Root	Het. Stationarity		Robust	Demeaned	-8.30*	0.00
$\Delta nec_t$	IPS	Hom. Unit Root	Het. Stationarity		Robust	Demeaned	-34.60*	0.00
$nec_t$	IPS	Hom. Unit Root	Het. Stationarity		Robust	Demeaned	-7.93*	0.00

Hadri and Im, Pesaran and Shin Panel unit root tests. Following the Dickey and Pantula approach, first differences are tested first. Upon non rejection of the null hypothesis, the test stops, otherwise it continues to levels.

## 4.7 Robustness analysis - Panel Unit Root

As we have stated previously, we have chosen Panel unit root tests to countercheck for the results of the stochastic time series persistence analysis on the basis of an inverted null, accountability of cross sectional dependence (and of course more common spherical disturbances), and heterogeneity of the alternative hypothesis. We remind that, similarly to the time series case, the ADF model test equation for the Panel unit root from Im, Pesaran and Shin (with a null of non stationarity and omitting panel specific trends) is:

$$\Delta nec_{i,t} = \xi_i nec_{i,t-1} + \epsilon_{i,t} \quad (4)$$

so that the homogeneous hypothesis will be  $H_0 : \xi_i = 0$  versus a heterogeneous null  $H_a = \xi_j < 0$ , where  $j \in [1 : i]$ . On the contrary, the LM statistic for the Hadri test, which presents a null of stationarity, is modelled as an LM test of the variances of a random walk with trend model and the random walk itself. Considering the model:

$$nec_{i,t} = w_{i,t} + \beta_i t + \epsilon_{i,t} \quad (5)$$

with random walk defined as:

$$w_{i,t} = w_{i,t-1} + \varepsilon_{i,t} \quad (6)$$

the test could be written as:  $H_0 : \vartheta = \frac{var(\epsilon_{i,t})}{var(\epsilon_{i,t})} = 0$  versus an alternative  $H_a : \vartheta > 0$ . Given the random walk collapses to a constant if its variance is 0, the model would become almost deterministic with an i.i.d. stochastic component, and the series would be automatically trend stationary. Logically, the null implies stationarity, not unit root behavior

The results of Hadri's second generation unit test for the whole country are thus available in Table 10, as well as the results of the Im, Pesaran and Shin first generation unit root test. The outcome of the analysis strongly rejects the unified null of stationarity and opts to point out at the alternative, heterogeneous possibility that some units (cross sections) might indeed be integrated.



## 5 Asymmetries - Panel Linearity Tests

Having found initial evidence of the hysteresis phenomenon, we investigate whether additional nonlinearity could be found in the relationship between such variable and unemployment. Before switching our attention to threshold regressions, we need to test for linearity against a nonlinear alternative through the well established Hansen test as seen in its smoothed variant in Gonzales et al.. We ought to remind that in our estimation strategy, the afore-mentioned test is intended to give us evidence of possible regime-wise nonlinearity, making us feel more comfortable as we proceed to select nonlinear models and comparing them among themselves and the base linear model focusing exclusively on a measure of fit (an information criteria, in our case). In this whole panel pre-test, the test equation, based on an ADF reparametrization of the necessity entrepreneurs series, contains smoothing component which mimics with a logistic function a smooth dummy variable (Equation 7):

$$\Delta nec_{i,t} = \alpha_i + \lambda_t + \beta'_1 nec_{i,t-1} + (\beta''_2 nec_{i,t-1}) * G(u_{i,t}; \gamma; \theta) + \varepsilon_{i,t} \quad (7)$$

the test requires substituting  $G(s_{i,t}; \gamma; c)$  with its first order Taylor expansion centered around  $\gamma = 0$ . (as we just explained, Hansen extended to Panel). Generalizing the expansion to up to  $m$  regimes, we would get Equation 8:

$$\Delta nec_{i,t} = \mu_i + \beta'_0 * nec_{i,t} + \beta'_1 * nec_{i,t} q_{i,t} + \dots + \beta'_m * nec_{i,t} q_{i,t}^m + u_{it}^* \quad (8)$$

with its null based on the joint nonsignificance of all the coefficients of the branches of the regression, which is equivalent to set the slope of function  $G$  equal to 0 in Equation 9

$$H_0 : \beta'_1 * = \dots = \beta'_m * = 0 \simeq H_0 : \gamma = 0 \quad (9)$$

Given how delicate this first a priori test is in giving us an idea of how much a generic nonlinear alternative could perform against the null of absolute linearity, we choose to bootstrap the test results around one hundred times. Furthermore, at this stage of the draft, the test against any homogeneous alternative has been done at the panel level, for an autoregressive (a la ADF) specification with an attractor and with the unemployment rate as the switching variable. The battery of tests (LM, F and HAC corrected based on the joint null of each coefficient of each regime (from zero to a maximum of two) generally held favorable indication of possible nonlinearity in the opportunity entrepreneurs group, pointing at the possible existence of at least a pair of regimes. The very same result was detected for the joint panel hypothesis of no statistical difference between segment slopes for the necessity group, with a p value comfortably close to five percent in all five tests we specified, efficiently rejecting the null of absolute linearity at the overall panel level. The results we have just commented on are readily available in Table 11. Even though a time series based Hansen test or any other given test of linearity against general nonlinearity might be

Table 11: Linearity tests against one or two regime models. Alternative tests.

$nec_t$	$m$	$LM(x)$	$p\text{-value}$	$LM(F)$	$p\text{-value}$	$HAC(X)$	$p\text{-value}$	$HAC(F)$	$p\text{-value}$
$nec_t$	$0vs1$	8,303	0,004	8,190	0,004	3,461	0,063	3,414	0,065
	$0vs2$	12,420	0,002	6,120	0,002	3,470	0,176	1,710	0,181
	$0vs1$	8,303	0,004	8,190	0,004	3,461	0,063	3,414	0,065
	$2vs1$	4,139	0,042	4,080	0,044	1,887	0,170	1,860	0,173
$opo_t$	$m$								
	$0vs1$	16,250	0,001	16,030	0,001	3,396	0,065	3,350	0,067
	$0vs2$	16,370	0,001	8,066	0,001	4,862	0,088	2,396	0,091
	$0vs1$	16,250	0,001	16,030	0,001	3,396	0,065	3,350	0,067
	$2vs1$	0,117	0,001	0,116	0,001	1,793	0,181	1,767	0,184

Heteroskedasticity consistent LM and F tests.

used to investigate each and every region at the sectorial level, this a priori unified outcome is thus granting us enough evidence to proceed with the choice of more specific threshold functional forms at such lower level of detail.

## 6 Threshold Regressions

In order to give the reader an idea of the models of choice, let's focus on a generic TAR first, adjusting it to our case: an unrestricted, **three regimes TAR**, but with an ADF specification, would look something like this:

$$\Delta nec_t = \begin{cases} c_1 + \rho_l nec_{t-1} + e_t & \text{if } u_t \leq \theta_l \\ c_2 + \rho_m nec_{t-1} + e_t & \text{if } \theta_l \leq u_t \leq \theta_h \\ c_3 + \rho_h nec_{t-1} + e_t & \text{if } u_t \geq \theta_h \end{cases} \quad (10)$$

With  $nec_t$  necessity entrepreneurs at time  $t$ ,  $u_t$  unemployment level,  $\theta$  threshold value of  $u$ , and  $e_t$  hopefully (i.i.d.). Of course, if  $\theta_l = \theta_h$ , with  $\rho_l = \rho_m = \rho_h$  the model collapses to  $\Delta nec_t = \rho nec_{t-1} + e_t$ , and we are back to the linear case. By any chance, we also would want to specify an unrestricted three regimes SETAR, where the self exciting component is represented by the contemporaneous value of the objective variable. Following on to the example in Equation 10 and targeting the opportunity entrepreneurs series, we would similarly have:

$$\Delta opo_t = \begin{cases} c_1 + \rho_l opo_{t-1} + e_t & \text{if } opo_t \leq \theta_l \\ c_2 + \rho_m opo_{t-1} + e_t & \text{if } \theta_l \leq opo_t \leq \theta_h \\ c_3 + \rho_h opo_{t-1} + e_t & \text{if } opo_t \geq \theta_h \end{cases} \quad (11)$$

### 6.1 Thresholds autoregressions (Autonomous Communities)

In this section, we run a series of threshold autoregressions on a series of ADF type models of order 1 (obtained by subtracting  $y_{t-1}$  to both sides of a random walk with drift process). This way, with (mainly) first differenced stationary variables, the value of the attractor will give us an idea of how fast the recovery is from the shock (how grave the hysteresis phenomenon is) subject to variations in the unemployment rate, which remained our threshold variable. We will evaluate in this case both the level value of the unemployment and its first difference. That will tell us whether the absolute value of unemployment or its

Table 12: TAR regional models, Necessity entrepreneurs

<i>nec<sub>t</sub></i>	$\rho_l$	$\rho_m$	$\rho_h$	$\rho_{linear}$
(I)	(II)	(III)	(IV)	(V)
<i>Andalusia</i>	1,047*	-0,399*	-0,889*	-
<i>Aragon</i>	-0,678*	-	-1,018*	-
<i>Asturias</i>	-	-	-	-0,632*
<i>Balearic Islands</i>	-0,778*	-	0,110	-
<i>Canary Islands</i>	-0,424*	-	-1,434*	-
<i>Cantabria</i>	-	-	-	0,936*
<i>Castile and Leon</i>	-1,198*	-0,821*	-1,097*	-
<i>Castile-La Mancha</i>	-0,464*	-	-0,878*	-
<i>Catalonia</i>	-0,256*	-	-0,929*	-
<i>Valencian Community</i>	-0,645*	-	-1,107*	-
<i>Extremadura</i>	-0,438*	-	-1,191*	-
<i>Galicia</i>	-1,299*	-	-0,213*	-
<i>Community of Madrid</i>	-0,340*	-	-1,032*	-
<i>Region of Murcia</i>	-0,875*	-	-1,268*	-
<i>Navarre</i>	-0,735*	-	-1,370*	-
<i>Basque Country</i>	-	-	-	-0,795*
<i>La Rioja</i>	-0,966*	-	-1,007*	-
<i>SPAIN</i>	-0,147*	-1,206*	-0,882*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1 - \alpha)/(1 - \lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

short run variation matter more in terms of self employment choice. It is also worth noting that, different from, say, the Hansen test comparing linearity with some non specified form of (regime) nonlinearity through polynomial expansion, in this and the following paragraphs we shall consider goodness of fit as an a posteriori additional rule of choice comparing a linear representation of the decay against a multiple regime alternative. Rather than on the  $R^2$ , we shall focus on the BIC as the rule of choice.

Let's first consider unemployment as a threshold: In the case of necessity entrepreneurs, region 1 and 7 presented two distinct threshold (and thus three regimes), regions 3 6 and 16 were considered linear (no threshold could be found) while the rest of the regions showed a a suitable functional form a model with two regimes and a single threshold. Overall, the whole country (18) presents itself with two thresholds and three regimes.

Again, as we consider again unemployment in levels as our threshold variable and we switch our attention to opportunity entrepreneurs, we appear to be able to find a possible three regimes/two thresholds representation for 5 14 17 18 , a linear representation for 2 3 6 10 12 15 and a two regimes/one threshold representation for the rest of the countries.

Let's now consider the change in unemployment as our objective threshold: as we start with necessity once again, we notice how sensibility of the deviations to changes in unemployment is far lesser compared to sensibility to the overall magnitude of unemployment: only region 4 would present a model with three regimes and two threshold values, while only region 9 would show sign of a single threshold value with two regimes. It is however worth noting that the country as a whole (18) would present signs of nonlinearity, although bordering non-significance in the lower regime.

Finally, in the case of the opportunity entrepreneurs, 1 14 16 would present a three regimes model, 2 3 4 5 6 7 11 15 17 18 would be better represented by a linear model, while the rest would indicate a two regimes model as the best suitable fit for the data.

Table 13: TAR regional models, Opportunity entrepreneurs

<i>oport</i>	$\rho_l$	$\rho_m$	$\rho_h$	$\rho_{linear}$
(I)	(II)	(III)	(IV)	(V)
<i>Andalusia</i>	-1,152*	-	-0,495*	-
<i>Aragon</i>	-	-	-	-0,437*
<i>Asturias</i>	-	-	-	-0,517*
<i>Balearic Islands</i>	-0,450*	-	-1,179*	-
<i>Canary Islands</i>	-0,297*	-1,411*	-0,522*	-
<i>Cantabria</i>	-	-	-	0,723*
<i>Castile and Leon</i>	-1,285*	-	-0,408*	-
<i>Castile-La Mancha</i>	-0,130	-	-0,792*	-
<i>Catalonia</i>	-0,223*	-	-0,879*	-
<i>Valencian Community</i>	-	-	-	-0,365*
<i>Extremadura</i>	-0,465*	-	-0,798*	-
<i>Galicia</i>	-	-	-	-0,412*
<i>Community of Madrid</i>	-0,281*	-	-1,106*	-
<i>Region of Murcia</i>	-0,403*	-0,528*	-1,287*	-
<i>Navarre</i>	-	-	-	-0,965*
<i>Basque Country</i>	-1,168*	-	-0,549*	-
<i>La Rioja</i>	-0,475*	0,610*	-1,106*	-
<i>SPAIN</i>	-0,550*	-0,319	-0,768*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

## 6.2 Threshold autoregressions (Sectorial Level)

Before discussing the deviation values, it would be useful getting an equivalent overview at the sectorial level.. As we base our results on the previous section, we focus on the unemployment rate as a level threshold variable. Starting with the necessity entrepreneurs group, we found a suitable two regime representation for 1 4 6 9 10 14 16 18 and a suitable three regime representation for 7 8 12 and 15 in the agricultural sector. As we moved on to the industry sector, we found a good fitness for a two regime model in 8 and 9 and a three regime model in 11 13 16 18. Moving on to the construction sector, regions 2 4 7 8 10 12 14 15 17 and 18 were found to fit better two regimes, while no regions could be more efficiently described by a 3 regimes model. In the service sector, the low qualified group presented a satisfying fitness, although restricted to two regimes only, for 4 5 7 9 12 13 14, while the three regimes one would be a valid alternative for 1 8 10 11 16 and 18. Finally, the high qualified service group had regions 1 2 5 6 8 9 14 15 well described by a two regimes transition model, ad region 4, 10, 13 and 18 by a three regimes model. It would thus appear the service sector would present much of the asymmetric variation and adjustment we would see in the bust and boom cycle of necessity self-employment.

Let's now switch our attention to the opportunity entrepreneurs group. As for the agricultural sector, 1 6 8 9 10 11 12 13 14 16 17 and 18 would show a suitable two regime modelling solution, while region 3 only would point at a three regimes structure. In the industrial sector, regions 1 2 7 8 9 11 12 14 15 16 would suggest a two regimes structure, while 10 and 18 would better welcome a three regimes model. In the constructions sector, regions 1 2 7 8 9 10 11 12 14 15 16 18 would fit better two regimes model, while region 5 only would better fit a model with two threshold values and two regimes. Switching to the low skilled service sector, regions 7 8 13 15 16 17 would present a two regimes model, while regions 1 4 6 9 10 14 18 would find a three regimes ones a better solution. This last one is perhaps the sector where the number of transitions equals 2 in more regions than those where it equals only one: that would point

Table 14: Necessity workers, agricultural sector, all accepted three regimes models

(I)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-1,251*	-	-1,117*	-
Aragon	-	-	-	-0,880*
Asturias	-	-	-	-0,883*
Balearic Islands	-1,061*	-	-0,897*	-
Canary Islands	-	-	-	-1,082*
Cantabria	-0,685*	-	-1,088*	-
Castile and Leon	-0,512*	-1,378*	-1,091*	-
Castile-La Mancha	-0,482*	-2,699*	-0,967*	-
Catalonia	-1,286*	-	-1,014*	-
Valencian Community	-0,866*	-	-0,861*	-
Extremadura	-	-	-	-0,583*
Galicia	-1,100*	-0,213*	-0,569*	-
Community of Madrid	-	-	-	-0,812*
Region of Murcia	-1,291*	-	-1,010*	-
Navarre	-0,701*	-1,52*	-1,039*	-
Basque Country	-0,583*	-	-0,908*	-
La Rioja	-	-	-	-0,844*
SPAIN	-0,430*	-	-0,455*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 15: Necessity workers, Industry sector, all accepted three regimes models

(I)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-	-	-	-1,097*
Aragon	-	-	-	-1,084*
Asturias	-	-	-	-1,025*
Balearic Islands	-	-	-	-1,084*
Canary Islands	-	-	-	-0,957*
Cantabria	-	-	-	-0,734*
Castile and Leon	-	-	-	-0,816*
Castile-La Mancha	-0,323*	-	-1,065*	-
Catalonia	-1,287*	-	-0,897*	-
Valencian Community	-	-	-	-1,086*
Extremadura	-0,731*	-0,291	-1,066*	-
Galicia	-	-	-	-0,764*
Community of Madrid	-0,659*	-1,768*	-1,263*	-
Region of Murcia	-	-	-	-1,094*
Navarre	-	-	-	-1,075*
Basque Country	-1,025*	-1,150*	-1,352*	-
La Rioja	-	-	-	-1,032*
SPAIN	-0,735*	-0,508*	-1,541*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 16: Necessity workers, Construction sector, all accepted three regimes models

(I)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-	-	-	-0,598
Aragon	2,622*	-	-1,041*	-
Asturias	-	-	-	-0,852*
Balearic Islands	-1,033*	-	-1,285*	-
Canary Islands	-	-	-	-0,842*
Cantabria	-	-	-	-0,926*
Castile and Leon	-1,076*	-	-0,992*	-
Castile-La Mancha	-0,917*	-	-0,861*	-
Catalonia	-	-	-	-0,581*
Valencian Community	-0,852*	-	-1,355*	-
Extremadura	-	-	-	-1,080*
Galicia	-1,108*	-	-0,634*	-
Community of Madrid	-	-	-	-0,869*
Region of Murcia	-0,971*	-	-0,948*	-
Navarre	-1,132*	-	-1,117*	-
Basque Country	-	-	-	-1,145*
La Rioja	-0,940*	-	-1,048*	-
SPAIN	-0,364*	-	-0,847*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 17: Necessity workers, Low skilled Service sector, all accepted three regimes models

(I)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-1,379*	-0,668*	-0,674*	-
Aragon	-	-	-	-0,908*
Asturias	-	-	-	-0,975*
Balearic Islands	-0,832*	-	-0,463	-
Canary Islands	-0,871*	-	-1,237*	-
Cantabria	-	-	-	-1,145*
Castile and Leon	-1,204*	-	-0,973*	-
Castile-La Mancha	-0,674*	-1,421*	-0,841*	-
Catalonia	-0,298*	-	0,739*	-
Valencian Community	-1,065*	-1,394*	-0,812*	-
Extremadura	-0,944*	-1,582*	-1,586*	-
Galicia	-1,384*	-	-0,679*	-
Community of Madrid	-0,742*	-	-0,914*	-
Region of Murcia	-0,993*	-	-1,337*	-
Navarre	-	-	-	-1,058*
Basque Country	-0,947*	-	-1,358*	-
La Rioja	-	-	-	-0,985*
SPAIN	-0,314*	-1,499*	-0,780*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 18: Necessity workers, High skilled Service sector, all accepted three regimes models

(I)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-0,445*	-	-1,170*	-
Aragon	-0,908*	-	0,999*	-
Asturias	-	-	-	-0,992*
Balearic Islands	-0,799*	-0,937*	-0,548*	-
Canary Islands	-0,700*	-	-1,521*	-
Cantabria	-0,853*	-	-1,827*	-
Castile and Leon	-	-	-	-1,028*
Castile-La Mancha	-1,103*	-	-0,619*	-
Catalonia	-0,624*	-	-1,467*	-
Valencian Community	-0,504*	-0,842*	-0,994*	-
Extremadura	-	-	-	-0,961*
Galicia	-	-	-	-0,770*
Community of Madrid	-0,319*	-1,138*	-1,158*	-
Region of Murcia	-1,184*	-	-0,975*	-
Navarre	-0,869*	-	-1,949*	-
Basque Country	-	-	-	-0,978*
La Rioja	-	-	-	-1,115*
SPAIN	-0,693*	-0,269	-1,271*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 19: Opportunity workers, agricultural sector, all accepted three regimes models

	$\rho_l$	$\rho_m$	$\rho_h$	$\rho_{linear}$
(I)	(II)	(III)	(IV)	(V)
Andalusia	-1,053*	-	-0,730*	-
Aragon	-	-	-	-0,867*
Asturias	-0,965*	0,352	-1,043*	-
Balearic Islands	-	-	-	-1,043*
Canary Islands	-	-	-	-0,985*
Cantabria	-0,480*	-	-1,199*	-
Castile and Leon	-	-	-	-0,692*
Castile-La Mancha	-0,575*	-	-1,081*	-
Catalonia	-0,753*	-	-0,750*	-
Valencian Community	-0,545*	-	-1,178*	-
Extremadura	-0,592*	-	-0,740*	-
Galicia	-0,377*	-	-1,088*	-
Community of Madrid	-0,966*	-	-1,007*	-
Region of Murcia	-0,766*	-	-1,366*	-
Navarre	-	-	-	-0,940*
Basque Country	-1,423*	-	-0,974*	-
La Rioja	-0,870*	-	-1,537*	-
SPAIN	-0,363*	-	-0,803*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 20: Opportunity workers, industry sector, all accepted three regimes models

	$\rho_l$	$\rho_m$	$\rho_h$	$\rho_{linear}$
(I)	(II)	(III)	(IV)	(V)
Andalusia	-1,421*	-	-1,066*	-
Aragon	-0,727*	-	-1,013*	-
Asturias	-	-	-	-0,809*
Balearic Islands	-	-	-	-1,037*
Canary Islands	-	-	-	-1,015*
Cantabria	-	-	-	-1,038*
Castile and Leon	-1,824*	-	-0,676*	-
Castile-La Mancha	-0,210	-	-0,885*	-
Catalonia	-0,794*	-	-1,056*	-
Valencian Community	-1,818*	0,451	-1,096*	-
Extremadura	-0,930	-	-0,986*	-
Galicia	-0,658*	-	-1,014*	-
Community of Madrid	-	-	-	-1,045*
Region of Murcia	-0,700*	-	-1,178*	-
Navarre	-1,018*	-	-0,755*	-
Basque Country	-1,202*	-	-0,756*	-
La Rioja	-	-	-	-0,699*
SPAIN	-0,822*	0,294	-0,941*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

out at the existence of intermediate values of unemployment for which the rate of return of the unconditional mean of self-employment either speeds down or is not even present (quasi unit root behavior in the internal regime). Finally, as we have a look at the service sector share compose of high skilled labor, we observe that regions 4 8 13 14 would accept a two regimes representation, while regions 1 5 9 10 17 18 would go for a three regimes one. It is perhaps important to point out how the sector with the smoother transitions (mind, in terms of numbers of regimes/threshold values, and not how sharp the transition is), is perhaps the service sector. Economic actors in the service market tend to adapt less abruptly to market news than their agricultural and industrial equivalents.

Table 21: Opportunity workers, construction sector, all accepted three regimes models

(1)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-1,294*	-	-0,754*	-
Aragon	-0,588*	-	-1,006*	-
Asturias	-	-	-	-0,721*
Balearic Islands	-	-	-	-0,985*
Canary Islands	-0,700*	-1,289*	-1,147*	-
Cantabria	-	-	-	-0,856*
Castile and Leon	-0,851*	-	-0,674*	-
Castile-La Mancha	-0,659*	-	-0,845*	-
Catalonia	-0,685*	-	-0,909*	-
Valencian Community	-0,333*	-	-1,015*	-
Extremadura	-1,583*	-	-0,833*	-
Galicia	-0,945*	-	-0,813*	-
Community of Madrid	-	-	-0,882*	-
Region of Murcia	-0,988*	-	-0,679*	-
Navarre	-1,408*	-	-0,901*	-
Basque Country	-0,885*	-	-0,939*	-
La Rioja	-	-	-	-0,978*
SPAIN	-0,614*	-	-0,400*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 22: Opportunity workers, Low skill Service sector, all accepted three regimes models

(1)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-0,797*	-0,726*	-1,120*	-
Aragon	-	-	-	-0,649*
Asturias	-	-	-	-0,579*
Balearic Islands	-0,812*	-0,501	-1,224*	-
Canary Islands	-	-	-	-0,808*
Cantabria	-0,835*	-0,481*	-0,915*	-
Castile and Leon	-0,291*	-	-0,947*	-
Castile-La Mancha	-0,253*	-	-0,898*	-
Catalonia	-0,0262*	-1,331*	-0,983*	-
Valencian Community	-0,448	-0,945*	-0,769*	-
Extremadura	-	-	-	-0,774*
Galicia	-	-	-	-0,593*
Community of Madrid	-0,531*	-	-1,275*	-
Region of Murcia	-0,622*	-0,975*	-1,349*	-
Navarre	-1,476*	-	-1,025*	-
Basque Country	-1,333*	-	-0,669*	-
La Rioja	-0,437*	-	-1,104*	-
SPAIN	-0,582*	-0,367	-1,135*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

Table 23: Opportunity workers, High skill Service sector, all accepted three regimes models

(1)	$\rho_l$ (II)	$\rho_m$ (III)	$\rho_h$ (IV)	$\rho_{linear}$ (V)
Andalusia	-1,127*	-1,371	-1,025*	-
Aragon	-	-	-	-0,746*
Asturias	-	-	-	-0,802*
Balearic Islands	-0,418*	-	-1,106*	-
Canary Islands	-0,461*	-1,591*	-0,842*	-
Cantabria	-	-	-	-0,869*
Castile and Leon	-	-	-	-0,736*
Castile-La Mancha	-0,416*	-	-1,353*	-
Catalonia	-0,251*	-1,072*	-1,027*	-
Valencian Community	-0,589*	-1,205*	-0,946*	-
Extremadura	-	-	-0,970*	-
Galicia	-	-	-	-0,656*
Community of Madrid	-0,554*	-	-1,110*	-
Region of Murcia	-0,348*	-	-0,951*	-
Navarre	-	-	-	-0,784*
Basque Country	-	-	-	-0,715*
La Rioja	-0,707*	0,276	-1,300*	-
SPAIN	-0,582*	-0,162	-1,060*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1-x)/(1-\lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.



## 7 Inference

### 7.1 Rate of decay of the shocks to self-employment, national level

We now calculate the rate of decay (lambda in terms of time) of an autoregressive process of order 1 with a lagged attractor from the series at the regional level. Considering our previous results, it appears more than sensible to offer the calculated time deviations based on the level threshold of unemployment.

Given the results obtained on Spain (18) at the most aggregated possible level in the previous section, we will discuss and calculate the rate of decay of the process for necessity and opportunity entrepreneurs with a three regimes structures for both, and compare it to the linear specification in each case. We remind the reader that, given the simple ADF specification of our test equation, the inverse formula required to calculate the half lives of the deviations will be:  $\lambda^T = (1 - x)/(1 - \lambda)$ .

Beginning with the necessity entrepreneurs, our significant coefficients of error corrections for the three branches (regimes) are thus: -0.15, -1.21 and -0.88 in the low, middle and high regime of unemployment. This corresponds, in the two most extreme regimes, to a decay of 1.70 and 0.24 quarters respectively, required to recover half the positive shock to unemployment the economy has sustained. Evidently, switching from a lower state to a higher state of unemployment causes three effects: as unemployment is lower than its “natural rate”, after a positive shock which increases the number of necessity entrepreneurs, the rate of adjustment back to equilibrium is relatively slow. As unemployment increases and gets close to its natural rate (say, the middle regime), the speed of adjustment starts to accelerate as deviations are compensated more quickly (the economy and its operators have had time to learn how to react to the “natural rate of unemployment”). However, as the unemployment rate increases above its calculated threshold value (which we have improperly called up until now “natural rate”) the speed of adjustment after a positive shock starts to slow down again, as more and more self employed operators cannot be reabsorbed once more into the economy as salary workers. The richness of the description offered by the model clashed with the linear value of the attractor, whose coefficient is close to 0,22.

On a similar note, but with a central region behaving with a bit of a unit root behavior the values for the significant lower and upper regime of the opportunity model are -0.55, and -0.77 respectively. The in the speeds of adjustment, which in quarters equals a half life of 0,90 and 0,46, follows a very similar story when compared to the necessity entrepreneurs group, with a higher half life in the high unemployment regime with respect to the low unemployment regime: this suggests us that pull factors might be far stronger than push factors in prolonged states of above the level unemployment. Pretty much in line with the linear ADF model for the necessity entrepreneurs, the speed of adjustment in the case of the opportunity entrepreneurs is again fixed around 0,22. That amounts to a rate of decay of around 1,54 quarters.

Table 24: All sectors, national level, all accepted three regimes models

<i>Variable</i>	<i>Regimes</i>			<i>Linear</i>
<i>nec</i>	$\rho_l$	$\rho_m$	$\rho_h$	$\rho_{linear}$
<i>Agriculture</i>	-0,430*	-	-0,455*	-
<i>Industry</i>	-0,735*	-0,508*	-1,541*	-
<i>Construction</i>	-0,364*	-	-0,847*	-
<i>Low Service</i>	-0,314*	-1,499*	-0,780*	-
<i>High Service</i>	-0,693*	-0,269	-1,271*	-
<i>opot</i>	$\rho_l$	$\rho_m$	$\rho_h$	$\rho_{linear}$
<i>Agriculture</i>	-0,363*	-	-0,803*	-
<i>Industry</i>	-0,822*	0,294	-0,941*	-
<i>Construction</i>	-0,614*	-	-0,400*	-
<i>Low Service</i>	-0,582*	-0,367	-1,135*	-
<i>High Service</i>	-0,582*	-0,162	-1,060*	-

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1 - \alpha)/(1 - \lambda)$ . Columns (4), (V) and (VI): estimates for the best BIC performing TAR model.

## 7.2 Rate of decay of the shocks to self-employment, sectorial level

How does the situation differ across sectors? A relevant achievement of the convergence analysis at the sectorial level, which is visible in Table 24 is that in no case a linear alternative was deemed superior to a regime model in any specification across all sectors when goodness of fit was compared via the Bayesian Information criteria: the analysis shows how across all sectors two to three regimes were considered and always performed better than the linear alternative. Focusing on the opportunity entrepreneurs group, Agriculture and Construction were the only sectors to be better suited by a two regime model, while Industry and both service sectors pointed at three regime modelling. In particular, and similarly to the result we obtained at the national level in Table 25, the former sectors showed the presence of what the literature on persistence would consider a form of "inaction band": as the coefficient governing the middle regime<sup>2</sup> is statistically imprecise and thus not so distant from 0, the opportunity entrepreneurs across sectors would not converge neither diverge to its mean as the model would collapse, for  $\rho_m = 0$ , to the benchmark random walk with drift. This would mean that, for values of unemployment inside such a "natural interval" in the middle of the regression model, the model would act in a quasi-unit root manner, and wander aimlessly as time goes by. The rest of the inference base on the values of the branches which appear statistically significant do not appear to tell us a story any different from the aggregated case: higher speed of adjustment back to the equilibrium in the upper regime, where unemployment is at a higher threshold level, slower speed of adjustment in the lower regime, the only possible exception made for constructions where the opposite would happen (-0,614\* in the lower regime as opposed to -0,400\* in the upper regime).

<sup>2</sup>-0,31(0,18) at the national level, close to such value at the Sectorial level, ranging from -0,162 in High Skill Services to -0,367 in Low Skill Services.

Table 25: Speed of convergence estimates, AR(1) and BEST TAR

	<i>ADF(1)</i>		<i>TAR</i>	
	$\rho$ (II)	$\rho_{l,quarters}$ (III)	$\rho_{m,quarters}$ (IV)	$\rho_{h,quarters}$ (V)
$\Delta nec_t$		-0,15* (0,07)	-1,21* (0,23)	-0,88* (0,27)
$\Delta nec_t$	-0,22 (0,07)			
$\Delta opo_t$		-0,55* (0,10)	-0,31 (0,18)	-0,77* (0,27)
$\Delta opo_t$	-0,23 (0,07)			

Estimates of the attractors/error correction parameters,.

Table 26: Half life estimates, AR(1) and BEST TAR

	<i>ADF(1)</i>		<i>TAR</i>	
	$\lambda$ (II)	$\lambda_{l,quarters}$ (III)	$\lambda_{m,quarters}$ (IV)	$\lambda_{h,quarters}$ (V)
$\Delta nec_t$		1,70	0,42	0,24
$\Delta nec_t$	1,56			
$\Delta opo_t$		0,90	-	0,46
$\Delta opo_t$	1,54			

Half-life estimates of the attractors/error correction parameters, calculated according to  $\lambda^T = (1 - x)/(1 - \lambda)$ .

## 8 Conclusions

We have found out that a form of stochastic persistence exists in the conditional average value of the opportunity and necessity entrepreneurs groups. The hysteresis phenomenon can as such be proved at the regional level once the heterogeneous effects of different economic structures across regions have been taken into account. Apart from time-wise dependence, we also tested for alternative forms of nonlinearity of the series. We could prove, at the aggregated panel level, that an alternative form of regime driven nonlinearity exists in both groups and can be framed by imposing unemployment as a weakly exogenous variable acting as a threshold between different regimes of convergence. As we looked for the best functional form, we have finally seen how multiple branch regressions models such as the threshold autoregression model describe asymmetries with a better fit than the linear ADF specification in a number of regional cases, while non negligible differences in terms of speed of adjustment can be found across economic sectors.

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